# ECO 209Y
# Macroeconomic Theory and Policy

# Lecture 3:
# Aggregate Expenditure and Equilibrium Income

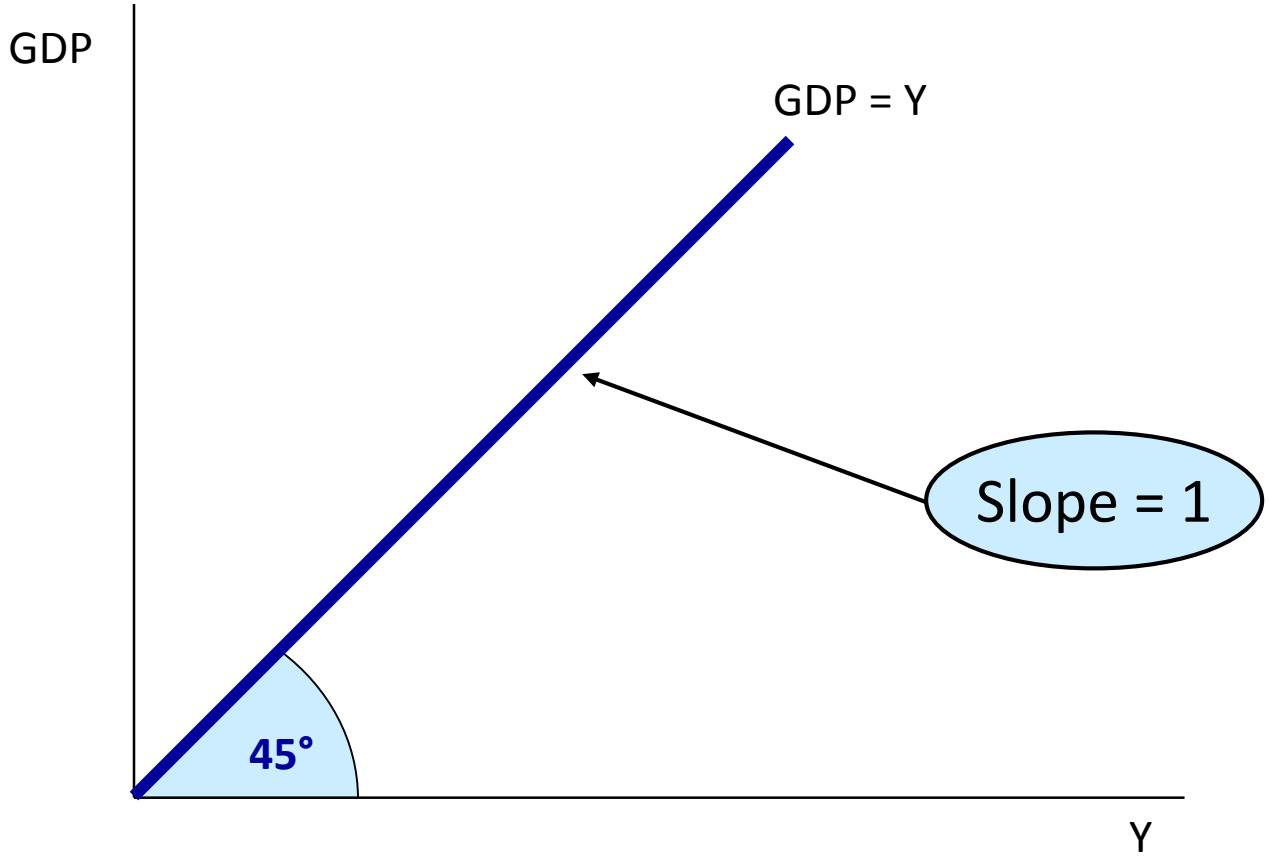
# ASSUMPTIONS

- We will assume that:
  - There is no ***depreciation***
  - There are no ***indirect taxes***
  - Net payment to foreign factors of production is nil

- Therefore, ***GDP***, ***Net Domestic Income*** , and ***Gross National Product*** are all equal

- In other words, the values of ***output*** and ***income*** are assumed to be equal and we will use the notation **Y** to refer to both

# Graphical Representation of GDP = National Income (Y)



# ASSUMPTIONS (CONT'D)

We will also assume that the ***price level*** (**P**) is fixed

- Therefore, this model applies to a situation where the economy is in a ***deep recession*** characterized by ***excess capacity*** and ***high unemployment***
- That is, we will consider the so-called short-run ***Keynesian model***

# Aggregate Expenditure

- ***Aggregate Expenditure*** (**AE**) is the total ***desired*** or ***planned*** expenditure on goods and services in the economy, that is:

$$AE = C + I + G + NX$$

- Using the expenditure approach, we have seen that **GDP** was equal to:

$$Y = C + I + G + NX$$

- **GDP** is equal to the ***actual*** expenditure on domestically produced goods and services
  - Therefore, ***actual*** expenditure on domestically produced goods and services is equal to ***income*** (**Y**) by assumption
  - Note that ***actual*** investment expenditure includes involuntary changes in inventory

# AGGREGATE EXPENDITURE (CONT'D)

- The ***Aggregate Expenditure*** function indicates the desired level of expenditure at each level of income (**Y**)
  - The ***Aggregate Expenditure*** function is an ***increasing function*** of **Y**
- Therefore, there must be a level of income at which ***desired*** aggregate expenditure (**AE**) is equal to ***actual*** aggregate expenditure (**GDP** = **Y**)
- This level of income at which **Y = AE** is the ***equilibrium*** level of output or income (**Y***)
  - At **Y*** the ***goods market*** is in ***equilibrium***
  - The economy has produced (**Y**) exactly what economic agents were planning to purchase (**AE**)

# AGGREGATE EXPENDITURE (CONT'D)

- If **Y ≠ AE**, then the economy is not in equilibrium
  - If **Y > AE** → excess supply in the goods market
  - If **Y < AE** → excess demand in the goods market
- Since **P** is assumed fixed, then the implicit assumption is that **aggregate expenditure** determines the amount of goods produced in the economy
- That is, **Y** must change in order to match **AE** and restore equilibrium in the economy
  - **Y** must increase to eliminate an excess demand
  - **Y** must decrease to eliminate an excess supply

# A Simple Model

- Consider a simple model of an economy without government sector (**G = 0**) and without external sector (**X = Q = 0**)
- Therefore, **AE = C + I**
- How is equilibrium income (**Y***) determined in this economy?

# The Planned (or Desired) Consumption Function

- The ***planned consumption function*** is a description of the total planned personal consumption expenditure by all households in the economy

- Planned consumption expenditure depends on variables such as:
  - Disposable income
  - Wealth
  - Interest rates
  - Expectations about the future

# THE PLANNED CONSUMPTION FUNCTION

- ***Assumption:*** With the exception of ***disposable income***, all the variables that determine ***planned consumption*** will be assumed ***constant***

- ***Assumption:*** Therefore, ***planned consumption*** will be assumed to be a function of ***disposable income*** (**YD**):

$$C = \bar{C} + c\,YD$$

- This equation indicates that ***planned consumption*** is equal to some constant ($\bar{C}$) plus another constant (**c**) times disposable income (**YD**)

# THE CONSUMPTION FUNCTION (CONT'D)

- The constant $\bar{C}$ describes the elements of consumption which are ***independent*** of disposable income
  - The constant $\bar{C}$ is called ***autonomous consumption*** and captures the impact on **C** of all the constant variables

- The constant **c** describes the ***rate of change*** of consumption as disposable income changes, that is, it indicates the increase in consumption per unit increase in disposable income:

$$c = \frac{\Delta C}{\Delta YD}$$

  - The constant **c** is called the ***marginal propensity to consume*** out of disposable income ($MPC_{YD}$)

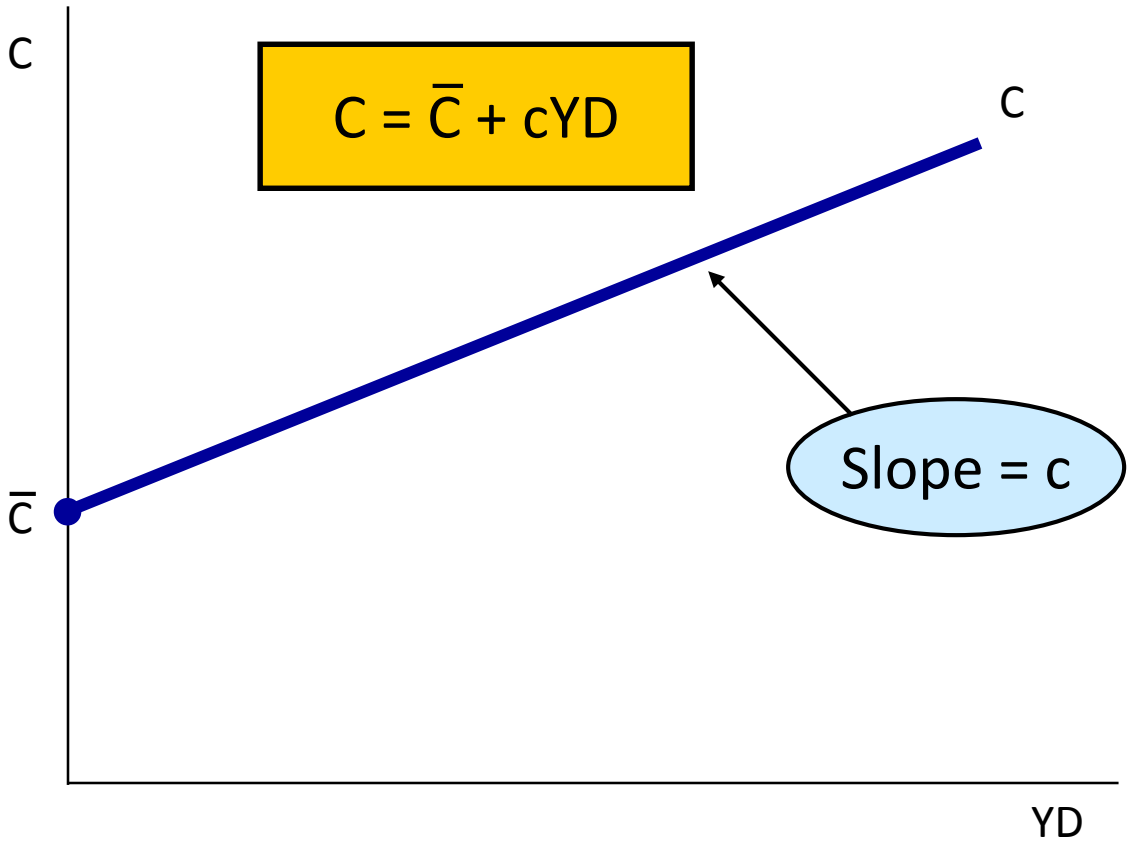
# Marginal Propensity to Consume

- Since we are assuming that there is no government sector, taxes (**TA**) and transfer payments (**TR**) are nil
  - Therefore, **YD = Y**
  - This means that consumption is assumed to depend on ***income*** (**Y**) alone:

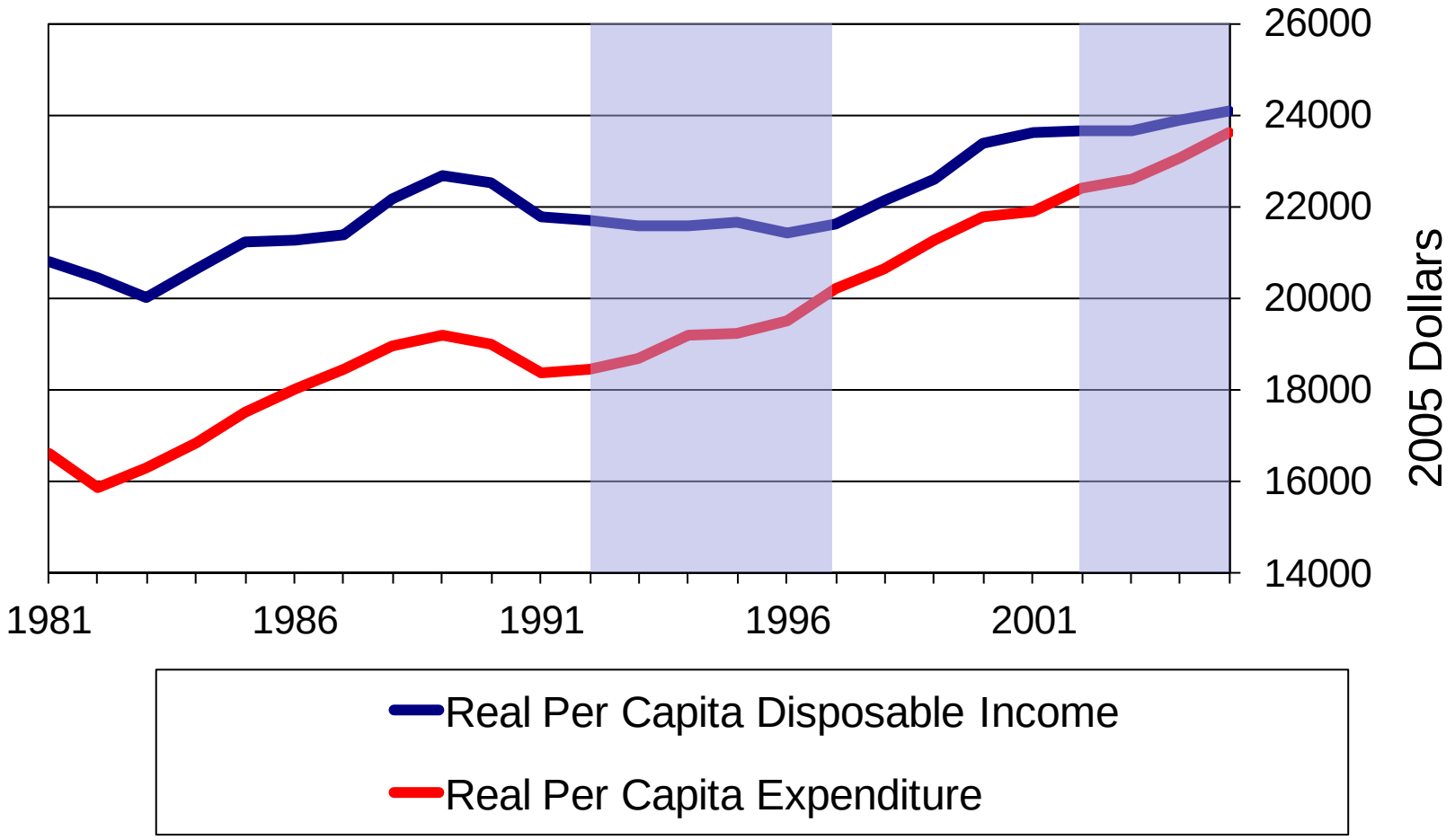
$$C = \bar{C} + cY$$

- Note that since **Y = YD**, then $MPC_Y = MPC_{YD}$
- However, as we will soon see, when **YD** differs from **Y**, $MPC_Y$ also differs from $MPC_{YD}$

# The Consumption Curve



# Canada: Per Capita Consumption and Disposable Income (1981-2005)



# Marginal Propensity to Save

- The **$MPC_{YD}$** is positive but less than 1, thus implying that a $1 increase in ***disposable income*** does ***not*** increase ***consumption*** by $1
- A fraction **c** is spent on consumption and the rest is saved (i.e., a fraction **s = 1 – c** is saved)
- The constant **s** is the ***marginal propensity to save*** out of disposable income (**$MPS_{YD}$**)
- Therefore, **c + s = 1**

# THE PLANNED SAVINGS FUNCTION

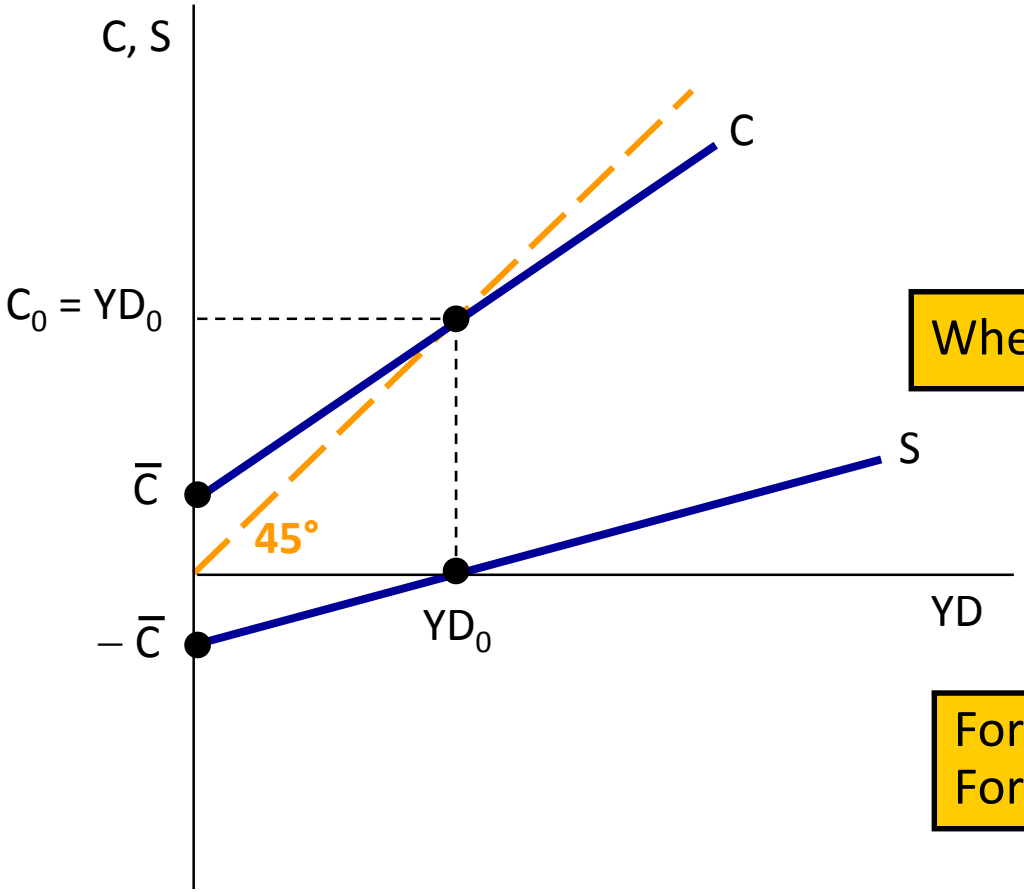
- Since **YD = C + S**, the ***savings function*** is given by:

$$S = YD - C$$
$$= YD - (\bar{C} + cYD)$$
$$= -\bar{C} + (1 - c)YD$$
$$= -\bar{C} + sYD$$

- Note that the $MPS_{YD}$ is also positive and less than 1 since $s = 1 - c$

- The ***savings function*** is sort of the mirror image of the consumption function

# CONSUMPTION AND SAVINGS FUNCTIONS




$$C = \overline{C} + c\,YD$$
$$S = -\overline{C} + (1 - c)\,YD$$

When YD = 0, then $C = \overline{C}$ and $S = -\overline{C}$

At the level of YD at which the C curve intersects the 45° line, C = YD and thus S = 0.

For $YD < YD_0$, $C > YD$ and thus $S < 0$.
For $YD > YD_0$, $C < YD$ and thus $S > 0$.

# THE PLANNED INVESTMENT FUNCTION

- The ***investment function*** is a description of the total (desired or planned) investment expenditure by all private economic agents in the economy

- In general, planned investment expenditure depends on:
  - The ***real*** rate of interest
  - The level of economic activity (**Y**)
  - Businesses' ***expectations*** about the behaviour of these variables during the lifetime of the investment

- I would argue that ***expectation*** about **Y** (and therefore about ***future demand***) is the most relevant variable determining investment

# THE PLANNED INVESTMENT FUNCTION

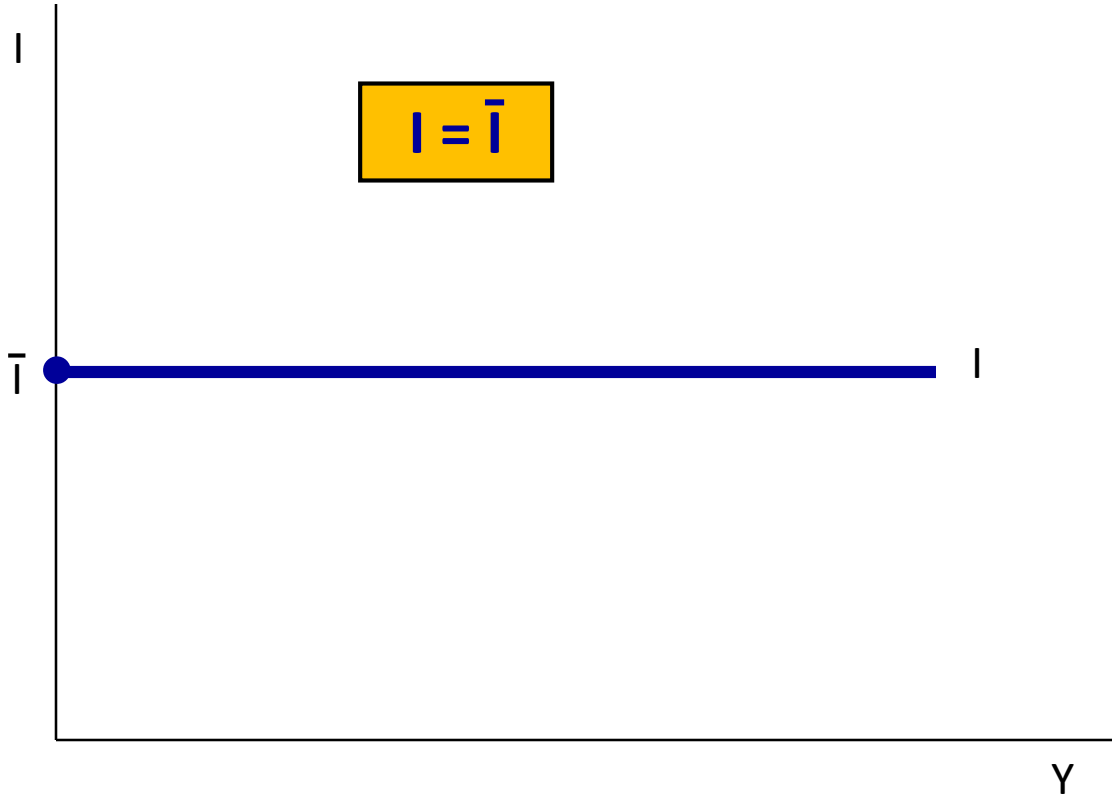
- ***Assumption:*** For simplicity, we will ***assume*** that the rate of interest and expectations about the future are constant

- ***Assumption:*** For simplicity, we will further ***assume*** that planned investment is independent of the level of income (**Y**)

- ***Assumption:*** Therefore, ***planned investment*** will not change as the level of income (**Y**) changes

  - **I** is equal to autonomous investment: $\mathbf{I = \bar{I}}$

# The Investment Curve



# THE AGGREGATE EXPENDITURE FUNCTION

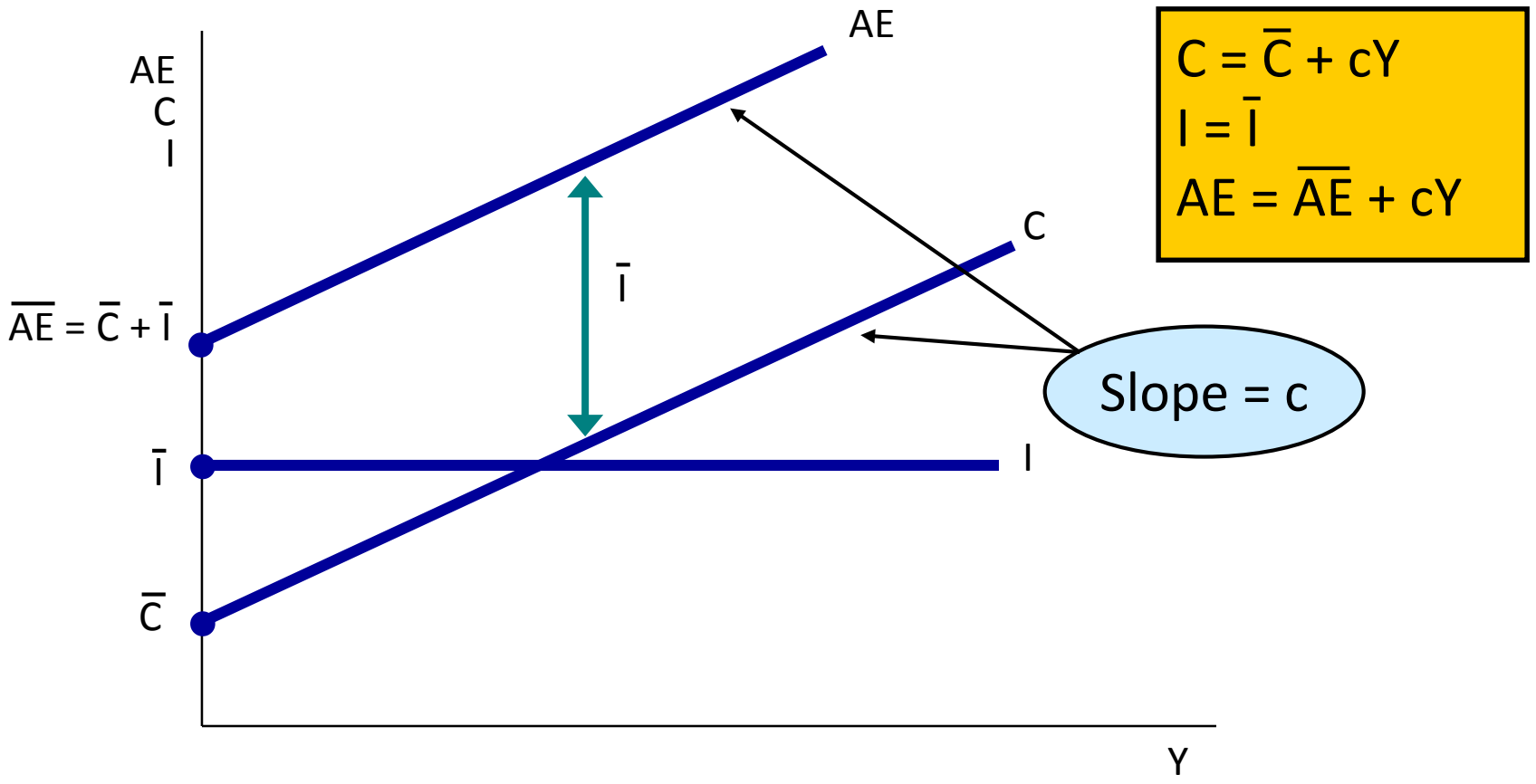
- In this very simple model, the ***aggregate expenditure*** function is:

$$\begin{aligned} AE &= C + I \\ &= (\bar{C} + cY) + \bar{I} \\ &= (\bar{C} + \bar{I}) + cY \\ &= \overline{AE} + cY \end{aligned}$$

  where $\overline{AE} = \bar{C} + \bar{I}$ is ***autonomous*** aggregate expenditure and **cY** is ***induced*** aggregate expenditure

- $\overline{AE}$ is the vertical intercept of the **AE** function, and **c** is the slope of the **AE** function (or the ***marginal propensity to spend***)

# Aggregate Expenditure Function



# EQUILIBRIUM INCOME AND OUTPUT

- We have seen that in ***equilibrium***, ***output*** (**GDP**) or ***income*** (**Y**) is equal to ***aggregate expenditure*** (**AE**):

$$Y = AE$$
$$= \overline{AE} + cY$$

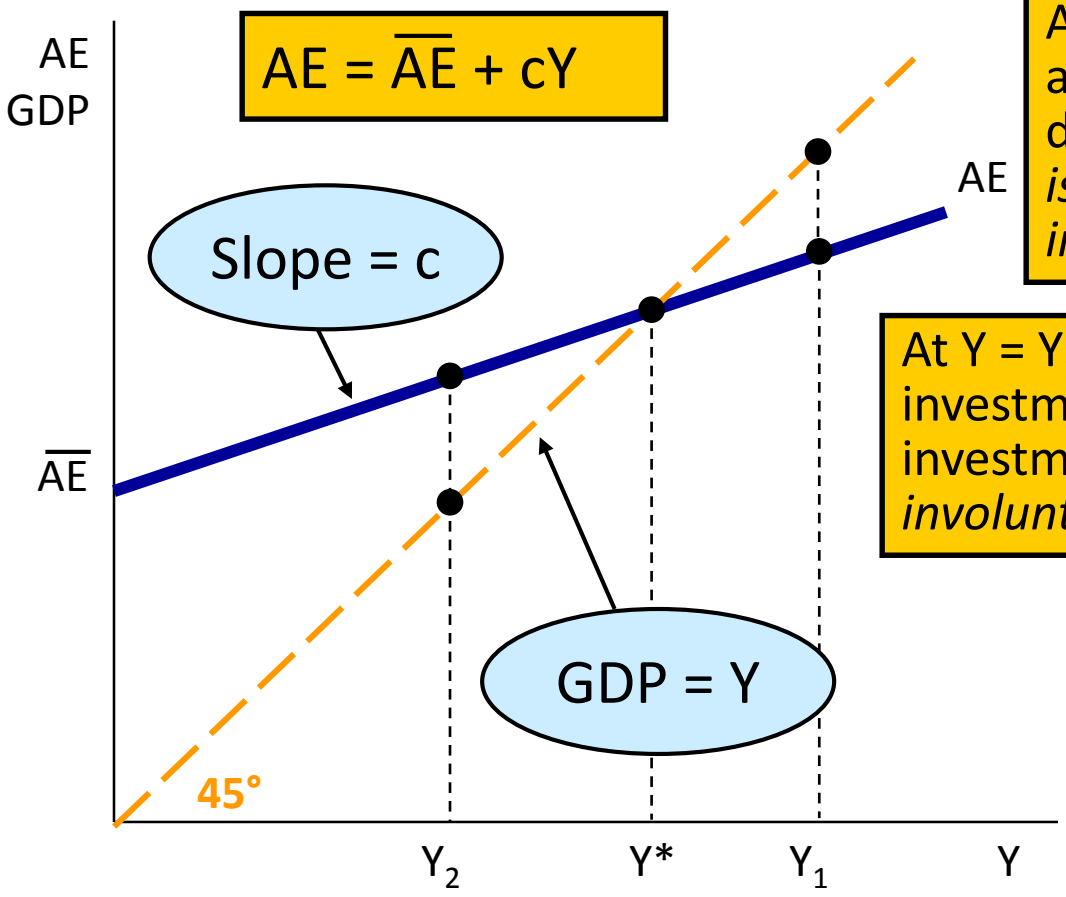
- Therefore, $Y - cY = \overline{AE}$

$$(1 - c)Y = \overline{AE}$$

and ***equilibrium income*** is:

$$Y^* = \frac{1}{1 - c}\,\overline{AE}$$

# AGGREGATE EXPENDITURE FUNCTION




At Y = Y*, Y = AE and thus actual investment is equal to desired investment → *There is no involuntary change in inventories*.

At $Y = Y_1$, Y > AE and thus actual investment is greater than desired investment → *There is an involuntary increase in inventories*.

At $Y = Y_2$, Y < AE and thus actual investment is smaller than desired investment → *There is an involuntary decrease in inventories*.

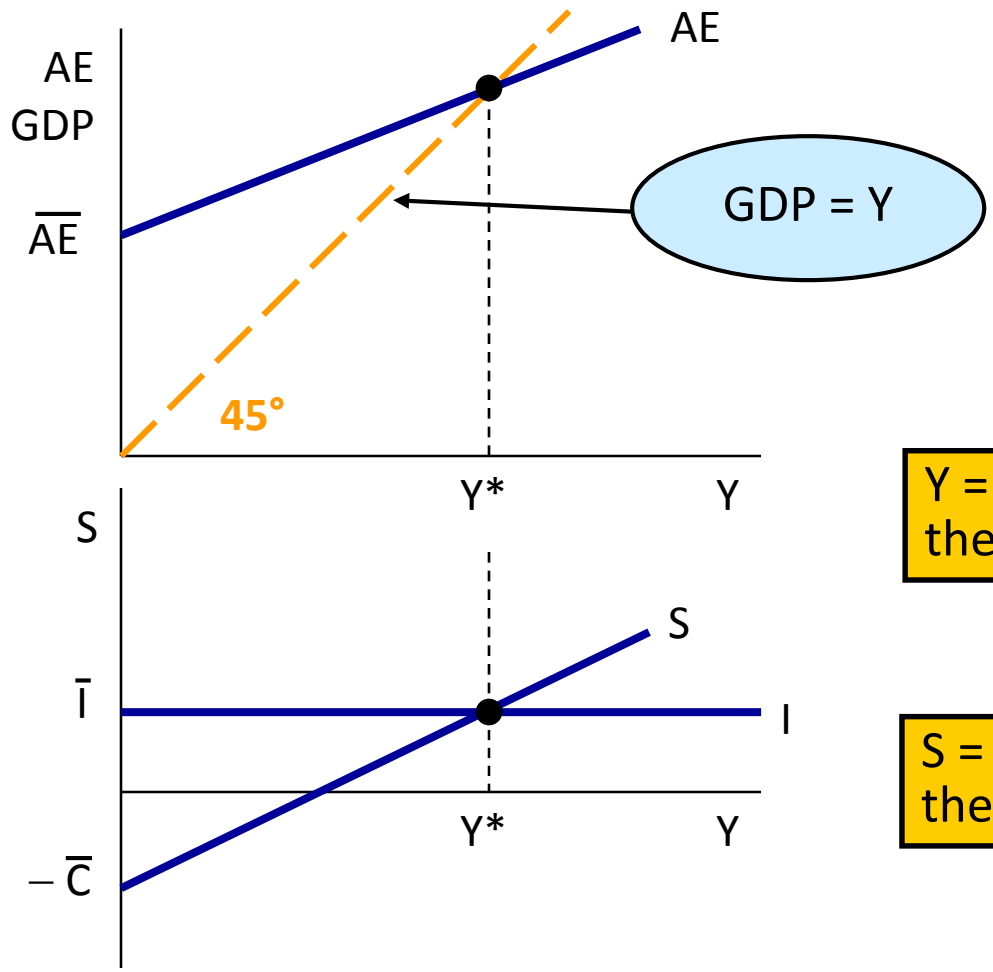
# CONSUMPTION AND SAVING

- The implicit ***assumption*** is that ***actual*** consumption is always equal to ***desired*** consumption as a result of ***involuntary*** changes in inventory
  - If **AE > Y**, there is an ***involuntary*** decrease in inventory to satisfy the level of desired consumption
  - If **AE < Y**, there is an ***involuntary*** increase in inventory because desired consumption is not enough (i.e., saving is too large)
- Therefore, since ***actual*** consumption and ***desired*** consumption are always equal, then ***actual*** saving and ***desired*** saving are always equal as well

# SAVINGS AND INVESTMENT

- By definition, ***savings*** is equal to ***actual investment***
  - Output (**GDP**) is equal to income (**Y**) by assumption
  - Income not spend on consumption is saved
  - Output not used for consumption is used for investment
- **Y = C + S** and **Y = C + *actual* I → S = *actual* I**
- In equilibrium, when **Y = AE**, there is no ***involuntary*** change in inventory
  - Therefore, ***desired*** and ***actual*** investment are equal
- Therefore, in a closed economy with no government sector,
  - If **Y = AE**, then **S = desired I**
  - If **Y < AE**, then **S < desired I**
  - If **Y > AE**, then **S > desired I**

# Two Ways of Expressing Equilibrium Income in the Economy




$S = -\overline{C} + (1 - c)Y$
$I = \bar{I}$
$AE = \overline{AE} + cY$

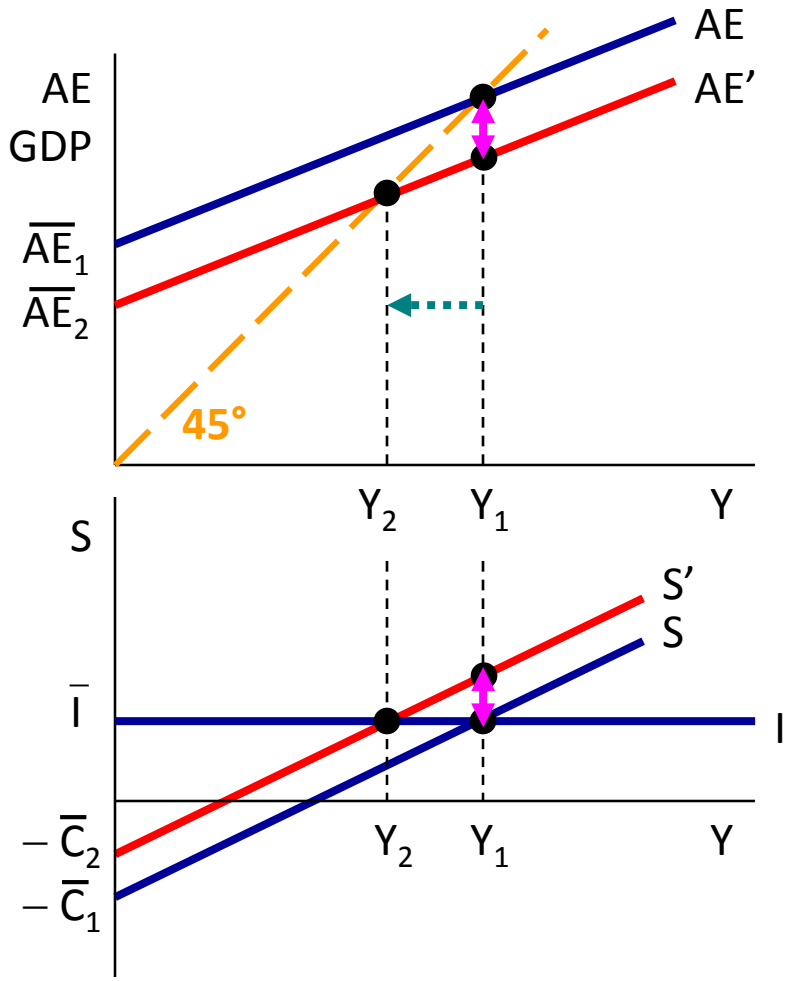
Y = AE at Y = Y*, and thus Y* is the equilibrium level of income.

S = I at Y = Y*, and thus Y* is the equilibrium level of income.

# SAVINGS AND INVESTMENT

- By definition, ***savings*** is always equal to ***actual investment***
- **Question:** If high rates of ***investment*** are desirable, are high rates of ***savings*** also desirable?
  - If ***productive*** investment were determined by savings, then high rates of savings would be desirable
- But ***high desired savings*** is the result of ***low desired consumption expenditure***
  - Therefore, ***actual investment*** is large because firms are experiencing ***involuntary*** increases in inventory
- Therefore, ***higher desired savings*** does not translate into ***higher productive capacity*** of the economy
  - But ***higher desired investment*** does translate into ***higher*** **Y** and thus into ***higher desired savings***

# SAVINGS AND INVESTMENT (CONT'D)




$S = -\overline{C} + (1 - c)Y$

$I = \bar{I}$

$AE = \overline{AE} + cY$

Initially the economy is in equilibrium at $Y_1$.

As desired savings increases to S' and aggregate expenditure decreases to AE', Y > AE and Y falls.

# The Multiplier

$$Y^* = \frac{1}{1 - c}\,\overline{AE}$$

- How does a change in ***autonomous expenditure*** ($\overline{AE}$) affect ***equilibrium income*** ($Y^*$)?
- The equation for equilibrium income shows that a $\Delta\overline{AE}$ will affect $Y^*$ in the following way:

$$\Delta Y^* = \frac{1}{1 - c}\,\Delta\overline{AE}$$

- The expression

$$\alpha_{AE} = \frac{\Delta Y^*}{\Delta\overline{AE}} = \frac{1}{1 - c} = \frac{1}{1 - \text{slope of AE curve}}$$

is called the ***autonomous expenditure multiplier*** or just the ***multiplier***

# THE MULTIPLIER (CONT'D)

- A change in autonomous expenditure ($\Delta\overline{AE}$) causes equilibrium income ($Y^*$) to change by the initial change in $\overline{AE}$ times the multiplier ($\alpha_{AE}$)
- This change in $Y^*$, $\alpha_{AE}\,\Delta\overline{AE}$, is the ***final result*** and does not show the ***process*** leading to it
- Let's have a look at the process leading to this final outcome
- Suppose that autonomous expenditure increases by $\Delta\overline{AE}$

# PROCESS OF ADJUSTMENT

| Round | ΔAE this round | ΔY this round | Accumulated ΔY |
|---|---|---|---|
| 1 | $\Delta\overline{AE}$ | $\Delta\overline{AE}$ | $\Delta\overline{AE}$ |
| 2 | $c\ \Delta\overline{AE}$ | $c\ \Delta\overline{AE}$ | $(1+c)\ \Delta\overline{AE}$ |
| 3 | $c^2\ \Delta\overline{AE}$ | $c^2\ \Delta\overline{AE}$ | $(1+c+c^2)\ \Delta\overline{AE}$ |
| 4 | $c^3\ \Delta\overline{AE}$ | $c^3\ \Delta\overline{AE}$ | $(1+c+c^2+c^3)\ \Delta\overline{AE}$ |
| … | … | … | … |
| n | $c^{n-1}\ \Delta\overline{AE}$ | $c^{n-1}\ \Delta\overline{AE}$ | $[1/(1-c)]\ \Delta\overline{AE}$ |

# PROCESS OF ADJUSTMENT (CONT'D)

- After **n** rounds, the series $1 + c + c^2 + c^3 + \ldots$ converges to $\alpha_{AE} = 1/(1 - c)$
- Let's call $a = 1 + c + c^2 + c^3 + \ldots$
- Multiply **a** by **c** → $ca = c + c^2 + c^3 + \ldots$
- Now subtract **ca** from **a**:

  $a - ca = (1 + c + c^2 + c^3 + \ldots) - (c + c^2 + c^3 + \ldots) = 1$
- Therefore, $a(1 - c) = 1$ → $a = 1/(1 - c)$

# Introduction of the Government Sector

- Disposable income (**YD**) changes:
  - Households pay ***taxes***
  - Households receive ***transfer payments***

- Equation for **AE** changes:
  - **AE = C + I + G**

- We will assume that ***government expenditure*** on goods and services is ***independent*** of the level of income, that is, **G** is ***fixed*** → **G = $\overline{G}$**

# Disposable Income and the Consumption Function

- We have seen that consumption is a function of **disposable income** (**YD**):

$$C = \bar{C} + cYD$$

where $\bar{C}$ is autonomous consumption and **c** is the ***marginal propensity to consume*** out of ***disposable income*** ($MPC_{YD}$)

- Disposable income (**YD**) is equal to:

$$YD = Y + TR - TA$$

where **TR** are ***government transfer payments*** and **TA** are ***direct taxes***

# Disposable Income and the Consumption Function (cont'd)

- Let's assume that taxes are a function of income and that transfer payments are independent of income:
  - $TA = \overline{T} + tY$
  - $TR = \overline{TR}$

- Therefore, disposable income is equal to:

$$YD = Y + TR - TA$$
$$= Y + \overline{TR} - (\overline{T} + tY)$$
$$= \overline{TR} - \overline{T} + (1 - t)Y$$

# The Consumption Function as a Function of Income

- As a function of ***income***, the consumption function is:

$$C = \bar{C} + cYD$$

$$YD = \overline{TR} - \bar{T} + (1 - t)Y$$

$$= \bar{C} + c\,[\,\overline{TR} - \bar{T} + (1 - t)Y\,]$$

$$= (\bar{C} + c\overline{TR} - c\bar{T}) + c(1 - t)Y$$

- That is, $(\bar{C} + c\overline{TR} - c\bar{T})$ is the vertical intercept and $c(1 - t)$ is the slope
- Note that $c(1 - t)$ is the ***marginal propensity to consume*** out of ***income*** ($MPC_Y$)
- Also note that $MPC_Y < MPC_{YD}$ if $t > 0$

# THE AGGREGATE EXPENDITURE FUNCTION

- The ***aggregate expenditure*** function is:

$$AE = C + I + G$$

$$= [\ \bar{C} + c\bar{TR} - c\bar{T} + c(1 - t)Y\ ] + \bar{I} + \bar{G}$$

$$= \bar{AE} + c(1 - t)Y$$

where $\bar{AE} = \bar{C} + c\bar{TR} - c\bar{T} + \bar{I} + \bar{G}$

- The vertical intercept is $\bar{AE}$ and the slope is $c(1 - t)$

- Recall that the slope of the **AE** curve is the ***marginal propensity to spend***

# Equilibrium Output and Income

- Equilibrium income is determined where **Y = AE**:

$$Y = \overline{AE} + c(1 - t)Y$$

$$[\ 1 - c(1 - t)\ ]\ Y = \overline{AE}$$

- Therefore,

$$Y^* = \frac{1}{1 - c(1 - t)}\ \overline{AE}$$

# The Multiplier

- The ***autonomous expenditure multiplier*** becomes:

$$\alpha_{AE} = \frac{1}{1 - c(1 - t)}$$

- Note that as before, the multiplier is equal to 1 over 1 minus the slope of the **AE** curve

- Also note that, as **t** increases, $\alpha_{AE}$ becomes smaller (the **AE** curve becomes flatter)

  ↳ What's the economic explanation?

# The Introduction of the Foreign Sector

- We will assume that the equations for ***exports*** (**X**) and ***imports*** (**Q**) are as follows:

$$X = \bar{X}$$

$$Q = \bar{Q} + mY$$

where **m** is the ***marginal propensity to import***

- Therefore, the equation for ***net exports*** (**NX**) is:

$$NX = X - Q$$

$$= \bar{X} - \bar{Q} - mY$$

# The Equation for the AE Curve

$$NX = \bar{X} - \bar{Q} - mY$$

- In a closed economy, the equation for AE was:

$$AE = C + I + G$$
$$= \overline{AE} + c(1 - t)Y$$

where $\overline{AE} = \bar{C} - c\bar{T} + c\overline{TR} + \bar{I} + \bar{G}$

- In an open economy, the equation for **AE** is:

$$AE = C + I + G + NX$$
$$= \overline{AE} + [c(1 - t) - m]Y$$

where $\overline{AE} = \bar{C} - c\bar{T} + c\overline{TR} + \bar{I} + \bar{G} + \bar{X} - \bar{Q}$

# Equilibrium Income

- In equilibrium, $Y = AE$, that is,

$$Y = \overline{AE} + [c(1 - t) - m]Y$$

$$\{1 - [c(1 - t) - m]\} Y = \overline{AE}$$

$$[1 - c(1 - t) + m] Y = \overline{AE}$$

- Therefore, equilibrium income is:

$$Y^* = \frac{1}{1 - c(1 - t) + m} \overline{AE}$$

where $\overline{AE} = \overline{C} - c\overline{T} + c\overline{TR} + \overline{I} + \overline{G} + \overline{X} - \overline{Q}$

# The Multiplier

- The multiplier is:

$$\alpha_{AE} = \frac{1}{1 - c(1 - t) + m}$$

$$= \frac{1}{1 - \text{slope of the AE curve}}$$

- Where the ***slope*** of the **AE** curve (i.e., the ***marginal propensity to spend***) is the fraction of each additional dollar of income which is spent on ***domestically produced goods***