Algorithmic Attention and Content Creation on Social Media Platforms*

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Abstract

This paper develops a theoretical framework to examine how a social media platform allocates attention through recommendation algorithms and how this in turn shapes content creation and consumption. Creators and viewers, as the two sides of the algorithm, fall into different categories based on interest. Creators are also heterogeneous in ability. We show that a platform, to maximize advertisement revenue, optimally filters out low-ability creators, restricts the reach of medium-ability creators to relevant audiences only, and propagates viral content for high-ability ones at the expense of relevance. The attention a creator receives grows disproportionally in his ability and the popularity of his category. We show the source of the inefficiencies of the algorithm by contrasting it with a welfare-maximizing benchmark. We additionally study the effect of monetary transfers in the algorithm. Our framework offers insights into content production and matching in digital markets, giving rise to potential regulatory interventions.

Keywords: Social Media; Platform; Content; Attention; Mechanism; Mismatch JEL Codes: D81, D82, D83

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1 Introduction

Today, there are estimated to be more than 5 billion people globally who use social media, accounting for more than 62 percent of the world population. In the US, the share is even higher, at around 90 percent. The intensity at which people use social media is just as staggering as the number of users, if not more so. Americans, on average, clock in more than 2 hours per day. Teenagers hit almost 5 hours, with 90 percent of their time spent on Youtube, TikTok and Instagram. Accordingly, advertisers spend more than 100 billion USD in the United States alone on social media and influencer advertising.

Social media platforms not only connect content creators with viewers, but through the design of their algorithms decide what viewers see and how much attention content creators receive.¹ Although recommendation algorithms have been instrumental in driving the influence and success of social media, the dominance of algorithmically curated content in users' feeds has not been universally welcomed. When Instagram moved to recommended content in 2022, Kylie Jenner, then the world's most followed person on Instagram, expressed her frustration about the social media platform's move by sharing a post that said "Make Instagram Instagram again. (Stop trying to be Tiktok, I just want to see cute photos of my friends)." The dominance of recommended content has not only led to discontent among content consumers (viewers), but also among creators, whose content is shown to others only if the algorithm decides so. In 2022, this has led a Tik-Tok influencer with thousands of followers to complain on Reddit, another social media platform, asking "What's the point of having TikTok followers?" (Reddit, 2022).

At the same time, social media platforms make money from advertising. A user scrolling through their Instagram feed inevitable encounters sponsored content regularly, that is, posts (or reels) which are only shown because an advertiser paid Instagram to target the user. To maximize advertising revenue, however, the platform cannot show viewers just ads. Rather, the algorithm needs to blend ads with high quality content of creators that viewers like, or else viewers would leave the platform. To incentivize content creators, in turn, the algorithm must allocate them a certain level of viewers' attention, or else creators would not spend effort to make content. Thus, a social media platform faces a two-sided mechanism design problem.

In this article, we study how a social media platform solves this mechanism design problem and characterize the platform-optimal recommendation algorithm (mechanism). In addition, we consider the welfare-optimal algorithm, allowing us to identify the distortions and inefficiencies created by the platform's profit-maximization incentive. The latter

¹On Instagram, the Reels and the Explore tab are exclusively for recommended content. Even the user's feed, which before 2022 was exclusively reserved for followed content, "will have a mix of content from the accounts you've chosen to follow, recommended content from accounts we think you'll enjoy and ads" an official instagram blogpost explains (Instagram Announcement, 2022). On Tiktok, recommended content is even more prominent.

improves our understanding of which regulation and behavioral measures can raise the welfare of viewers and content creators. Finally, we study how introducing monetary transfers between the platform and creators affects the optimal recommendation algorithm. Youtube has been relying on creator payments for a long time, and Tiktok has recently experimented with this too (see WSJ, 2024).

Our analysis reveals three main findings. First, the profit-maximizing algorithm crowds out low-ability content creators, forces intermediate-ability creators to exert too much effort, and induces viewers to spend excessive time on the platform. Our analysis thus makes an important contribution to the public debate about whether people spend too much time on social media.² Second, our analysis provides a profit-maximization rationale of the recent phenomenon of social media content "going viral," which took off after said platforms switched to an algorithm-led approach. Specifically, we show that to maximize profits from advertising, the platform optimally chooses to show already popular content to disproportionally many viewers, including viewers not interested in the content. Third, transfers from the platform to content creators fully eliminate irrelevant content from the viewers' feed if and only if selling ads is sufficiently lucrative for the platform (compared to the value content creators derive from receiving attention).

Our analysis builds on a novel model of social media that allows content creators to choose the effort they put into producing content and viewers to decide whether to pay attention to the recommended content. In the model, an algorithm is a mechanism that determines the content that each viewer sees (the viewer's "feed"), and the attention that each content creator receives. Content creators are horizontally differentiated in that creators focus on different topics, which vary in popularity among viewers. In addition, content creators differ in their ability to create high quality content. Content creators care about receiving attention from viewers.⁴ Viewers vary in what topic they are interested in. We accordingly quantify the popularity of a topic by the mass of viewers interested in it. The platform wants to maximize the total attention paid to ads, which it sells for a fixed price in the advertising market. Ads can be blended in the viewer's feed together with the creators' content. Both producing content and paying attention to it is costly. Therefore, the platform needs to satisfy the following two sets of obedience constraints: (i) each viewer's feed yields the viewer weakly positive utility so that viewers pay attention to

²A large and growing literature in social sciences studies the effect of social media on well-being. Allcott et al. (2020) find that disconnecting from social media in an experiment improves subjective well-being. Braghieri et al. (2022) find similar results, and further suggest that one of the mechanisms is related to social comparisons (the fear of receiving fewer likes than others).³ In another controlled experiment by Collis and Eggers (2022), the authors do not find any effect of reducing social media usage on well-being. However, in that study subjects in the treatment group used other apps on their smartphone more heavily (instant messaging), which could be detrimental for well-being as well.

⁴This assumption reflects intrinsic or extrinsic motivation from monetizing attention via deals with advertisers. However, Toubia and Stephen (2013) show that intrinsic motivation plays an important role for social media users. Similarly, Lindström et al. (2021) show that the desire for attention on social media follows a pattern of "reward learning, comparable to the behavior of animals in seeking rewards.

it, and (ii) each creator receives sufficient attention to motivate his production of high quality content.⁵

Intuitively, if the platform has access to higher quality content by creators, this relaxes the viewer's obedience constraint. As a result, the platform can blend more ads into the viewer's feed. To incentivize the costly production of high quality content, however, the platform needs to reward producers with more attention. The platform thus faces a tradeoff: allocate attention directly to ads or to content producers to incentivize the production of higher quality content, which then allows it to show more ads. For creators who are sufficiently popular or high in ability, the platform finds it profitable to do the latter. This relaxes the obedience constraint of a larger mass of viewers, eventually allowing the platform to show even more ads.

This implies distortions on both user sides of the platform. Some content creators exert more effort than they would if their content were recommended only to viewers who are in fact interested in their content. Conversely, viewers see content they are not interested in – in addition to ads – thus lowering their overall utility from consuming their feed. Thus, the fact that social media platforms earn money from selling ads not only affects viewers because it means viewers are exposed to ads, but it also because it distorts the platform's recommendation algorithm toward recommending irrelevant content.

That the platform thrives on irrelevant content recommendations also explains why certain content is made viral, i.e., shown to all viewers regardless of the viewers' interests. While showing the content of popular creators to all viewers lowers some viewers' utility from reading their feed, this boosts the utility of popular creators and allows the algorithm to extract more effort from them.⁶ This, in turn, relaxes the obedience constraint of the viewers interested in those creators' topics, of whom there are many since the platform makes mostly creators with popular topics go viral. Those viewers, therefore, can then be shown more ads, whereas the platform shows more irrelevant content to a smaller mass of viewers interested in less popular topics. In other words, the irrelevant content has a non-linear effect on profit after this feedback loop. As a result of this feedback loop, the number of ads shown to a viewer depends on their type. Viewers interested in less popular topics see fewer ads because the platform finds it more profitable to steer their attention toward content creators of popular categories to raise the effort of these creators. Due to the increased quality of content by popular creators, the platform can then expose viewers interested in that popular content to more ads.

⁵In the model, the platform perfectly observes quality as well as each viewer's and creator's type. In practice, social media platforms learn quality through experimentation, and user characteristics from machine learning. For example, to determine the quality of content, social media platforms reportedly show it only to a small group of users, whose engagement with said content is used as a proxy for quality. Our analysis abstracts from this experimentation phase.

⁶Note that popular here means that the creator focuses on a popular topic. That those creators become eventually popular in the true sense is endogenous to the algorithm and not assumed ex ante.

Finally, we highlight that if the value of ads is high, then inefficient recommendations of irrelevant content arise only if the platform is unable to pay creators. Compared to the algorithm that directs some of a viewer's attention to irrelevant (from a certain viewer's point of view) but popular content creators, showing the viewer an ad instead means less total attention that the platform can allocate to those popular creators. With transfers, however, the platform can provide alternative incentives. In particular, if the platform earns more for directing a unit of attention to an ad than the content creators value one unit of attention, then it is more profitable to incentivize the content creator with payments rather than attention from viewers who deem their content irrelevant.

In sum, our model rationalizes common behaviors related to social media. First, with the advent of TikTok in the US, which pioneered the heavy use of recommended content on users' feeds, a new phenomenon started on college campus (and other places): groups of young adolescents spending hours together to film content for the platform, hoping the algorithm will help their video go viral.⁷ Our model predicts that the profit-maximizing algorithm crowds out participation from low- to medium-ability content creators in favor of higher average content quality and increased advertisement exposure. Second, allocating too much attention to already popular content is part of the optimal algorithm. This explains the growing number of content creators whose content is distributed to millions of viewers as well as the phenomenon of viral content in general. Third, the profit-maximizing algorithm leads to excessive time spent on the social media platform, which appears in line with the high reported average daily social media usage of 4.8 hours (among teenagers) in the US. As our analysis shows, the main reason for these distortions lies in the advertising-funded nature of social media. As it tries to show viewers more ads, social media needs to also ramp up the production of content, which, in turn, requires it to harvest even more attention from viewers.

We contribute to the growing literature that studies competition for attention on social media. Relatively early work by Iyer and Katona (2016) studies a model of social media in which the platform cannot directly control the flows of content and attention. Rather, the key feature of social media in their model is that a message can be sent to multiple receivers. The authors show that increasing the number of recipients (growing the social media platform) drives up effort of senders, but also leads to fewer people choosing becoming senders. Ghosh and McAfee (2011), by contrast, consider a platform that can design an algorithm to incentivize content production. Specifically, they allow for algorithms that exclude low quality content from producers who exert too little effort.⁸ Ben-Porat and Tennenholtz (2018) study recommender systems with strategic content creators

⁷Besides, this anecdotal evidence, data show that the share of teenagers (its heaviest users) creating content on tiktok indeed very high at almost 80 percent .

⁸The platform relies on collecting engagement data from users to learn about the quality of content. They derive an algorithm which maximizes the average quality on the platform while keeping the number of instances when users see a low quality post for the purpose of learning the post's quality as small as possible.

as well but consider different objectives of the algorithm (e.g., fairness). Importantly, in those papers, the recommendation algorithm does not affect the total supply of attention, nor is the goal to maximize profits from advertising.

Closest to our work is the analysis by Qian and Jain (2024). They study the interaction of social media recommendation algorithms with endogenous content creation and revenue-sharing plans between influencers and the platform. Their main result is that the platform may want to bias its recommendation in favor of high-quality content even if it is less relevant. There are several differences between their analysis and ours. First, they fix the number of content creators and put a cap on content consumption, making it is impossible to assert the welfare distortions of the platform's algorithm, which is our focus. Second, our model features rich heterogeneity among viewers and content creators, allowing us to characterize agents' equilibrium participation, content production and consumption and outcomes for different types of creators and viewers. This allows us to assess the distributional impact of targeted regulatory interventions.

More generally, we contribute to the literature on advertising-funded media platforms (see, e.g., Anderson and Coate, 2005; Peitz and Valletti, 2008). More broadly, our research is related to two-sided markets research (see Jullien et al., 2021, for an excellent overview). The two-sided market literature typically considers platforms that charge at least one group of users for access to the other side of the market (e.g., advertisers). Since social media platform also charges advertisers, this work is closely related to ours. However, our focus lies on moderating the exchange between content creators and viewers, neither of which pay a monetary fee. Notable exceptions are from Bhargava (2022) and Ren (2024), who explicitly model the three-sided nature of social media platforms. Bhargava (2022) analyzes the optimal level of ads permitted by the platform and the optimal revenue sharing mechanism given endogenous content supply decisions. Relatedly, Ren (2024) studies advertising policies on decentralized content creation and examine its implications on designing advertising and revenue-sharing. However, these authors do not study the design of the optimal algorithm.⁹

Other work on social media includes Filippas et al. (2023), who consider a model of social media platforms (e.g., facebook or Twitter) where users, rather than an algorithm, have full control over which users they interact with. They show that users form strategic links to attain more attention, and characterize patterns of such link formation between users. Those papers differ from ours in that we focus on the case where the platform can control the flow of attention between users through the design of a recommendation algorithm. Although not our focus, others have also studied the spread of misinformation through social media users and the ensuing polarization (e.g., Berman and Katona, 2020; Acemoglu et al., 2024).

⁹Rather than modeling an algorithm explicitly, they assume, for example, that utility of viewers increases in the average effort and mass of content creators joining the platform, or that higher quality content is always prioritized by default.

In our model, some content creators endogenously emerge as influencers due to the algorithm and we are agnostic about whether those influencers desire attention for monetary incentives or are intrinsically motivated. A small but growing literature focuses more on how influencers make money, and the trade-off the face when showing organic versus sponsored content, including Fainmesser and Galeotti (2021) and Mitchell (2021).

Notably, sellers, two-sided platforms, and intermediaries in general, frequently use recommendation algorithms in e-commerce setups as well. Bergemann and Bonatti (2024) study a platform that uses data to match heterogeneous consumers with multi-product sellers. A common finding in this literature is that the profit-maximizing algorithm not always recommends the best product to consumers. For example, Hagiu and Jullien (2011) argue that an information intermediary uses divert consumer search to gain higher consumer traffic and influence sellers pricing. Teh and Wright (2022) show that an intermediary has the incentive to steer the recommendation to influence the competition of upstream sellers on prices and commissions. Choi and Jeon (2023) analyze the platforms' design biases in a two-sided market. Peitz and Sobolev (2025) show when an intermediary recommends a welfare-reducing bad match to facilitate better surplus extraction from sellers, and Bar-Isaac and Shelegia (2022) consider when an intermediary steers consumers to more profitable products. Janssen et al. (2023) study the profit-maximizing ranking algorithm of a search platform when consumers face search costs to inspect all options and find that the platform obfuscates the search results. De Corniere and Taylor (2019), Aridor and Gonçalves (2022) and Chen and Tsai (2024) study how an intermediary leverages biased recommendations to favor its own products when competing with third-party sellers. Ichihashi and Smolin (2023) and Condorelli and Szentes (2023) examine how recommendation algorithms can enhance consumers' countervailing power, shielding them from surplus extraction by sellers.

2 Model

2.1 Primitives

We model social media platform as a monopolistic two-sided online marketplace where users produce and consume digital content, such as articles, music, and videos. The platform employs a personalized recommendation algorithm to distribute content and advertisements to maximize its advertising revenue.

Creators and Viewers We consider two kinds of platform users: there are measure $m_c > 0$ of content creators and measure $m_v > 0$ of content viewers, which we call *creators* and *viewers* for short.

A creator is characterized by a two-dimensional type (θ, j) , where $\theta \in \mathbb{R}_+$ represents his ability, and $j \in \mathcal{N} \equiv \{1, ..., N\}$ indicates the horizontal category of a creator's contents. The proportion of type-*j* creators is denoted $\mu_j > 0$. The conditional distribution of θ given *j* is denoted by C.D.F. $F(\theta|j)$. For notation convenience, we assume $F(\theta|j)$ is differentiable for each (θ, j) .

For simplicity, we only account for horizontal heterogeneity among viewers and assume that every viewer is interested in only one content category. So, a viewer is labeled by $k \in \mathcal{N}$, the horizontal category that she is interested in.¹⁰ The proportion of type-kviewers is denoted $\nu_k > 0$.

Production, Ads, and Consumption Each creator of type (θ, j) can put in costly *effort* $e_j^{\theta} \ge 0$ to produce a unit of content, a post or a video for example. We assume that effort boots the *quality* of the content generated, not quantity. With effort level e_j^{θ} , creator type (θ, j) generates content of quality $q_j^{\theta} \equiv \theta e_j^{\theta}$, while incurring cost $c(e_j^{\theta})$. Therefore, the higher ability θ , the more efficient use of effort. As usual, we assume c(0) = c'(0) = 0 and c'(e), c''(e) > 0 for all e > 0. Moreover, c is assumed to be log-concave for normality.

Meanwhile, there is a competitive external market for *ads*. The platform can choose a non-negative amount of ads, blend them with the creators' contents, and make personal-ized recommendation to each viewer.

Each viewer of type k can spend *attention* on contents and ads that are recommended to them. Let $a_{j,k}^{\theta} \in [0, 1]$ denote viewer k's (unit) attention on creator (θ, j) 's content, and let $A_k \ge 0$ denote the attention on ads by viewer k. Attention is costly, and viewer k's total cost of reading contents and ads is:

$$t \cdot \left[m_c \sum_j \mu_j \int a_{j,k}^{\theta} \mathrm{d}F(\theta|j) + A_k \right],$$

where t > 0 is the unit cost of attention. In return, viewers derive ex post utility from reading contents (from entertainment or information, for example). A viewer *k*'s total benefit from reading is:

$$m_c \sum_j \mu_j \int a_{j,k}^{\theta} q_j^{\theta} \mathbb{1}\{j=k\} \mathrm{d}F(\theta|j) = m_c \mu_k \int a_{k,k}^{\theta} q_k^{\theta} \mathrm{d}F(\theta|k).$$

The benefit from each content depends on two factors: the quality q_j^{θ} and *relevance* (i.e., whether j = k or not). Here we make the simplifying assumption that reading *irrelevant content* $(j \neq k)$ yields zero utility, but this can be easily generalized. The benefit from watching ads is always zero.

¹⁰Similar results arise if we allow a viewer to be interested in multiple categories.

The platform profits from showing ads. The competitive market price for a unit of attention on ads is z > 0, so that the total profit of the platform reads:

$$zm_v \sum_k \nu_k A_k.$$

An important element of our model is that creators derive utility from the attention by viewers. In particular, a type- (θ, j) creator receives linear utility:

$$m_v \sum_k \nu_k a_{j,k}^{\theta}$$

from all attention received. The reduced-form specification captures creators' desire to gain online reach as it is the foundation of their psychological satisfaction, earning potential, influence, and career growth. In one extension we allow for explicit monetary transaction between the platform and the creators.

Platform Algorithm as Mechanism We model the algorithm of the social media platform as a recommendation mechanism. Formally:

Definition 1 (Algorithm)

An algorithm $\mathscr{A} \equiv (\tilde{a}, \tilde{A})$ consists of a content assignment $\tilde{a}_{j,k}^{\theta}(q) : \mathbb{R}_+ \times \mathcal{N}^2 \times \mathbb{R}_+ \to [0, 1]$ and an ads assignment $\tilde{A}_k : \mathcal{N} \to \mathbb{R}_+$.

The content assignment determines the probability of recommending (θ, j) 's content to type-k viewer, given the observed quality q. Remarkably, unlike ordinary commodities, digital content is *non-rival*: a creator's work can be consumed by an unlimited number of users simultaneously without diminishing its availability. Hence, we allow $\sum_k \tilde{a}_{j,k}^{\theta}(q) > 1$ for any j, θ, q . The ads assignment determines the measure of ads in the recommendation for type-k viewer. If some type stays out, the corresponding assignment is defined to be zero. The timeline is as follows.

- 1. The platform commits to the algorithm *A*, and then all creators and viewers simultaneously decide to join the platform or not. The outside option for all users is zero.
- 2. All creators (θ, j) who join the platform simultaneously put in effort e_j^{θ} to produce content of quality $q_i^{\theta} = \theta e_j^{\theta}$.
- 3. After seeing all q_j^{θ} , the algorithm sets $a_{j,k}^{\theta} = \tilde{a}_{j,k}^{\theta}(q_j^{\theta})$ and $A_k = \tilde{A}_k$. It then mixes contents and ads into a personalized recommendation set exclusive to viewer type $k, k \in \mathcal{N}$.

4. Each viewer *k* receives the recommendation set containing $a_{j,k}^{\theta}$ proportion of type (θ, j) 's content for all (θ, j) , along with a measure A_k of ads. All contents and ads are indistinguishable ex ante so that a viewer cannot cherry-pick. She chooses to read a share $\alpha_k \in [0, 1]$ of the recommendation set.

2.2 Model Discussions

The mechanism involves several important assumptions, which we discuss here. First, the platform can see the types of users as well as the quality of contents. This is because our model aims to characterize the long-run equilibrium instead of the transitory learning stage. With big data and long term interactions, a user's type is easily learned by algorithm. Quality is also mostly visible because a platform can hire a small set of test viewers or even AI to judge the quality of posts (Ghosh and McAfee, 2011).

Second, the assumption that content creators derive utility from attention is documented by a large empirical literature, and is also adopted in theory studies (e.g., Filippas et al., 2023). It explains why in many platforms with user-generated contents people voluntarily contribute even without direct monetary reward. For the purpose of this paper, we remain agnostic about the exact source of utility, be it psychological satisfaction or exogenous pecuniary benefits proportional to the creator's popularity.

Third, we assume that reading is an experience good. That is, viewers cannot cherrypick contents within the recommended set without incurring some attention costs. This assumption is mostly appropriate when it comes to static content such as short text or photos, because by the time viewers determines whether they like it or not, the attention is already spent. That is, there is little difference between evaluating and consuming it. Longer videos or texts, on the other hand, are different in that users can try to filter contents from the first few seconds of reading. However, such screening is far from perfect, as "click bait" on social media platform is all but rare. Oftentimes, viewers watch a video till the end, only to find that it is a scam or an embedded ad. As long as viewers cannot perfectly filter, the no-cherry-picking assumption is innocuous.¹¹ Moreover, trying to guess the quality by the sequence of recommended contents and ads is not effective, as the algorithm can always prevent it by randomizing the sequence.

Finally, in our model viewers can only read within their tailored recommendation. Notably, this does not forbid viewers from following creators of their choice; rather, the constraints is that viewers cannot read "followed content" exclusively. In reality, recommended content represents the lion's share of what people consume social medias such as Tiktok and Instagram, while "followed content" is in decline. These platforms even

¹¹Suppose the platform shows a viewer a mass A > 0 of ads if the viewer cannot cherry pick at all. Now suppose the user can detect and skip irrelevant content with probability 1/2, then the platform can just raise the mass of ads to 2A to achieve the same outcome.

start to weaken the "follow" function so that recommended contents and ads sneak in under the tab of "followed content."¹² In sum, the platforms realize the profitability of strengthening the algorithm and taking control of the attention flow. As such, we omit the "follow" function to simplify analysis.

3 Analysis

3.1 Simplifying the Problem

Revelation principle (Myerson, 1986) can further reduce the space of algorithms to *obedient algorithms* without loss of generality.

Definition 2 (Obedient Algorithm)

An obedient algorithm consists of an effort assignment $e_j^{\theta} : \mathbb{R}_+ \times \mathcal{N} \to \mathbb{R}_+$, a content assignment $a_{j,k}^{\theta} : \mathbb{R}_+ \times \mathcal{N}^2 \to [0,1]$ and an ads assignment $A_k : \mathcal{N} \to \mathbb{R}_+$, such that:

$$m_v \sum_k \nu_k a_{j,k}^{\theta} - c(e_j^{\theta}) \ge 0, \ \forall \ \theta, j,$$
(1)

$$m_c \mu_k \int \theta a_{k,k}^{\theta} e_k^{\theta} \mathrm{d}F(\theta|k) - t \cdot \left[m_c \sum_j \mu_j \int a_{j,k}^{\theta} \mathrm{d}F(\theta|j) + A_k \right] \ge 0, \ \forall \ k.$$
⁽²⁾

The first set of constraints, (1), are the obedience constraints for creators. When following the recommendation, their individual net utility must be greater than their individual rational payoff. This is so because the platform observes creator's ability and content quality, and whenever the realized quality does not equal θe_j^{θ} , the platform can use the harshest punishment $a_{j,k}^{\theta} = 0$ for all $k \in \mathcal{N}$, resulting in a non-positive net utility. The second set of constraints, (2), represents the obedience constraints for viewers. These constraints ensure that, for every viewer type, the marginal benefit of paying more attention to the recommended set always exceeds the marginal cost, making it optimal for them to fully consume the recommended content.

Lemma 1 (Revelation Principle)

For any equilibrium outcome induced by some algorithm, there exists an obedient algorithm inducing the same outcome.

¹²Similarly, on Quora and Reddit, ads and recommended threads are mixed among the pertinent contents.

Among obedient algorithms, the optimization problem can be written as:

$$\max_{\substack{\{e_j^{\theta}\}_{\theta,j} \ge 0, \{A_k\}_k \ge 0\\ \{a_{j,k}^{\theta}\}_{\theta,j,k} \in [0,1]}} zm_v \sum_k \nu_k A_k$$
s.t. (1), (2).

Next, we make two observations of the constraints. First, the obedience constraints (2) must be binding at optimum. If not for some k, then the platform should simply increase A_k to improve profits. Second, it is without loss of generality to require the obedience constraints (1) to be binding. If not for some creator type (θ, j) , then the platform can increase e_j^{θ} without violating the obedience constraints. This is summarized in the following lemma.

Lemma 2 (Binding Constraints)

There exists an optimal algorithm where the obedience constraint (1) *and the obedience constraint* (2) *are both binding.*

With the binding constraints, we can substitute e_j^{θ} and A_k , omit the positive multiplier $\frac{zm_c m_v}{t}$, and rewrite the problem as:

$$\max_{\substack{\{e_{j}^{\theta}\}\theta_{j} \geqslant 0\\ \{a_{j,k}^{\theta}\}\theta_{j}, j \in [0,1]}} \sum_{k} \nu_{k} \mu_{k} \int \theta a_{k,k}^{\theta} e_{k}^{\theta} \mathrm{d}F(\theta|k) - t \cdot \left[\sum_{k} \sum_{j} \nu_{k} \mu_{j} \int a_{j,k}^{\theta} \mathrm{d}F(\theta|j) \right]$$
(3)

s.t.
$$e_j^{\theta} = c^{-1} \left(m_v \sum_k \nu_k a_{j,k}^{\theta} \right), \ \forall \ \theta, j,$$
 (4)

$$\mu_k \int \theta a_{k,k}^{\theta} e_k^{\theta} \mathrm{d}F(\theta|k) - t \cdot \left[\sum_j \mu_j \int a_{j,k}^{\theta} \mathrm{d}F(\theta|j) \right] \ge 0, \ \forall \ k.$$
(5)

The objective (3) is the total ads inserted in the recommendation set of all viewers. If the total benefit from reading is higher than the total attention cost from reading contents, then there is room for the platform to sneak in more ads. The constraint (4) is a rewriting of the binding obedience constraint. The constraint (5) is the previous non-negativity constraint on A_k . It appears here because A_k is no longer an explicit variable in the optimization.

3.2 Optimal Algorithm

In this section we first solve the profit maximization problem for the platform, and then contrast it with a user welfare maximization problem of a hypothetical benevolent platform. We focus on the case of low attention cost, where t is sufficiently small but positive. This guarantees that the constraint (5) does not bind at optimum.

To understand the platform's trade off of attention allocation, we examine the impact of adjusting a_{jk}^{θ} on the platform's advertising revenue. To do so, we replace e_j^{θ} in (3) by constraint (4) and take first derivative with respect to a_{jk}^{θ} .

For some generic (θ, j, k) , if $q_j^{\theta} = \theta e_j^{\theta} = 0$, then the derivative of the objective with respective to $a_{j,k}^{\theta}$ is

 $-t\nu_k\mu_j f(\theta|j) < 0,$

regardless of whether k = j. This means if the quality of a content is zero, it is never optimal to allocate any attention, be it relevant or irrelevant. This is intuitive. If $q_j^{\theta} = 0$, it must be either because the creator's ability is $\theta = 0$ or because their effort level is $e_j^{\theta} = 0$. In the first case, allocating any attention to the creator has no incentive value. In the second case, since the creator's optimal effort is zero, there is no reason to allocate them any attention.

If $\theta e_j^{\theta} > 0$, however, the derivative of the objective with respective to $a_{j,k}^{\theta}$ reads (omitting positive multipliers):

$$-t + \theta e_{j}^{\theta} + \frac{\theta}{c'(e_{j}^{\theta})} m_{v} \nu_{j} a_{j,j}^{\theta} \quad \text{if } k = j,$$

$$-t + \frac{\theta}{c'(e_{j}^{\theta})} m_{v} \nu_{j} a_{j,j}^{\theta} \quad \text{if } k \neq j.$$

The intuition for the derivative is clear. If k = j, then recommending (θ, j) 's content to k has three effects on the quantity of ads. The first term, -t, is the attention cost on the content that crowds out attention on ads. The second term, θe_j^{θ} , is the quality of content, which is also the benefit from reading. This relaxes the obedience constraint and thus allows for more ads. The third term, $\frac{\theta}{c'(e_j^{\theta})}m_v\nu_j a_{j,j}^{\theta}$, is the most interesting force. By assigning attention, the creator receives higher utility, which in turn allows the platform to extract marginally $\frac{1}{c'(e_j^{\theta})}$ more effort. The increased effort then benefits all relevant viewers of mass $m_v\nu_j a_{j,j}^{\theta}$, amplified by the ability θ .

If $k \neq j$, then the second term is missing as the viewers do not benefit from reading irrelevant contents. Nevertheless, the third term is still there, meaning that recommending irrelevant contents is not a pure waste of time. By increasing the reach among irrelevant viewers, a creator gains from attention and is willing to work harder subject to the obedience constraint. The resulting higher quality content benefits relevant viewers and relaxes their obedience constraint, thereby admitting more ads. This explains why the algorithm may want to mismatch contents on purpose.

The comparison between the two cases implies that as long as a creator produces con-

tent of positive quality, it must first reach to all relevant viewers before starting to reach irrelevant ones. Formally, define

- $\overline{a}_{j}^{\theta} \equiv a_{j,j}^{\theta} \in [0, 1]$ as the *reach* among the relevant viewers, or the attention a type- (θ, j) creator receives from type-*j* viewers, and
- $\underline{a}_{j}^{\theta} \equiv \frac{1}{1-\nu_{j}} \sum_{k \neq j} \nu_{k} a_{j,k}^{\theta} \in [0, 1]$ as the *reach* among the irrelevant viewers, or the attention a type- (θ, j) creator receives from all viewers other than type j.

We conclude the following.

Lemma 3 (Priority)

(i) If $\overline{a}_{j}^{\theta} = 0$, then $\underline{a}_{j}^{\theta} = 0$; (ii) If $\underline{a}_{j}^{\theta} > 0$, then $\overline{a}_{j}^{\theta} = 1$.

Furthermore, the objective can now be simplified to:

$$\sum_{j} \mu_{j} \int \left(\nu_{j} \overline{a}_{j}^{\theta} \theta c^{-1} \left(m_{v} \nu_{j} \overline{a}_{j}^{\theta} + m_{v} (1 - \nu_{j}) \underline{a}_{j}^{\theta} \right) - t \left(\nu_{j} \overline{a}_{j}^{\theta} + (1 - \nu_{j}) \underline{a}_{j}^{\theta} \right) \right) \mathrm{d}F(\theta|j), \tag{6}$$

where $\overline{a}_j^{\theta} \in [0,1]$ and $\underline{a}_j^{\theta} \in [0,1]$ are the only choice variables, and

$$m_v \nu_j \overline{a}_j^{\theta} + m_v (1 - \nu_j) \underline{a}_j^{\theta}$$

is the total attention (also utility from attention) creator (θ, j) receives. The reformulation reveals that what matters for the optimal attention allocation for each creator type- (θ, j) are the received attention from the relevant viewers and the one from irrelevant viewers. Exactly how to allocate attention over different irrelevant viewer types has no impact. This observation substantially reduces the dimensionality of our optimization analysis.

The objective is concave in $\underline{a}_{j}^{\theta}$. This is because in the second term, irrelevant attention comes with a linear cost, while in the first term, it generates a marginally decreasing effect in extracting the creators. In contrast, the objective is convex in $\overline{a}_{j}^{\theta}$. While the second term is still linear in $\overline{a}_{j}^{\theta}$, the first term is convex as there is complementarity between the attention from a viewer and the effort of a creator. The more relevant attention, the more profitable squeezing effort from creators; the higher effort, the more profitable it is to allocate relevant attention. Therefore, the multiplicative term $\overline{a}_{j}^{\theta}c^{-1}(m_{v}\nu_{j}\overline{a}_{j}^{\theta} + m_{v}(1-\nu_{j})\underline{a}_{j}^{\theta})$ is convex, given the log-concavity of c.

Therefore, the optimal algorithm must display a bang-bang solution for the reach of relevant contents but could feature interior reach of irrelevant contents. Indeed, this is confirmed in the following statement of the optimal algorithm.

Proposition 1 (Optimal Algorithm)

Suppose the attention cost t is sufficiently low. For each category j, the optimal algorithm partitions abilities into four groups with cutoffs $0 < \theta_j^* < \theta_j^{\dagger} < \theta_j^{\ddagger}$: (1) If $\theta \leq \theta_j^*$, the creator is inactive, with $e_j^{\theta} = 0$, $\overline{a}_j^{\theta} = 0$ and $\underline{a}_j^{\theta} = 0$; (2) If $\theta_j^* < \theta \leq \theta_j^{\ddagger}$, the creator is a local producer, with $e_j^{\theta} = c^{-1}(m_v\nu_j)$, $\overline{a}_j^{\theta} = 1$ and $\underline{a}_j^{\theta} = 0$; (3) If $\theta_j^{\dagger} < \theta < \theta_j^{\ddagger}$, the creator is a fledgling influencer, with $e_j^{\theta} = c'^{-1}(\theta m_v \nu_j/t)$, $\overline{a}_j^{\theta} = 1$ and $\underline{a}_j^{\theta} = \frac{c(c'^{-1}(\theta m_v \nu_j/t)) - m_v \nu_j}{m_v(1-\nu_j)} \in (0, 1)$; (4) If $\theta \geq \theta_j^{\ddagger}$, the creator is a global influencer, with $e_j^{\theta} = c^{-1}(m_v)$, $\overline{a}_j^{\theta} = 1$ and $\underline{a}_j^{\theta} = 1$. The cutoffs are: $\theta_j^* = \frac{t}{c^{-1}(m_v \nu_j)}$, $\theta_j^{\ddagger} = \frac{tc'(c^{-1}(m_v \nu_j))}{m_v \nu_j}$, $\theta_j^{\ddagger} = \frac{tc'(c^{-1}(m_v))}{m_v \nu_j}$.

For each category j, the optimal algorithm sorts creators into four segments according to their ability θ . The ones with lowest ability are *inactive creators*, excluded from production because their effort hardly generates any synergy with their ability, which does not justify any attention away from ads. The ones with slightly higher ability are called *local producers*, who puts in the same effort in exchange for attention from and only from relevant viewers. The ones with even higher ability are called *fledgeling influencers* as they not only cater to relevant viewers but also project their influence onto some of the irrelevant viewers. The total attention a creator receives increases in his ability θ , but the utility increase in completely offset by the higher effort level required by the platform. Finally, the ones with the highest ability are called *global influencers*. Their contents penetrate the entire market, relevant and irrelevant alike. Figure 1 plots the total attention $m_v(\nu_j \overline{a}_j^\theta + (1 - \nu_j)\underline{a}_j^\theta)$ a type- (θ, j) creator receives in the optimal algorithm, where $c(e) = e^2$. Panel (a) shows the total attention as an increasing function of ability θ , while Panel (b) plots the total attention as an increasing function of the popularity ν_j of his own category.

As is evident from the optimal algorithm, the platform thrives on irrelevant content recommendations. While irrelevant content and ads are both worthless for the viewers, they serve different roles in the maximization. Ad is the way to cash out the viewers' positive net utility, if any, and has a linear effect on the profit. On the other hand, while irrelevant contents do not benefit the viewers, they boost the utility of the creators and allows the algorithm to extract more effort from them. This in turn relaxes the obedience constraint of the relevant viewers and makes room for more ads. In other words, the irrelevant content has a non-linear effect on profit after this feedback loop. This also explains why in the optimal algorithm, irrelevant attention increases in the ability θ or popularity ν_j . When assigning more irrelevant attention and extracting higher effort, it is the high- θ creators whose extra effort is most fruitful, and it is the creators in the popular category whose viewers benefit the most.

It is notable in Figure 1 that for fledgling influencers, the total attention grows faster than linearly. This implies that when we compare two creators in the same category, the



Figure 1: Effort and attention assignment in the optimal mechanism. Parameter: $c(e) = e^2$. Panel (a): Total attention received as function of ability θ , fixing *j*. Panel (b): Total attention received as function of popularity ν_j , fixing θ .

one with higher ability will gain disproportionally larger attention; the same is true when we compare two creators of the same ability but born in categories of different popularity.

Corollary 1 (Skewness)

For fledgling influencer of type (θ, j) , the total attention received is $c(c'^{-1}(\theta m_v \nu_j/t))$. Moreover, $\frac{c(c'^{-1}(\theta m_v \nu_j/t))}{\theta}$ increases in θ and $\frac{c(c'^{-1}(\theta m_v \nu_j/t))}{\nu_j}$ increases in ν_j .

Intuitively, a creator with higher ability or larger relevant audience are required to work harder, and due to the convex effort cost, the algorithm must allocate increasingly more attention to compensate the creators. This disproportional effect resonates well with the empirical finding that the attention distribution on the social platforms is skewed towards high-ability creators and popular categories.

Finally, we would like to discuss the sustainability of categories. Suppose the distribution of ability θ has a bounded support on $[0, \overline{\theta}_j]$ for category $j, j \in \mathcal{N}$. In order for any creator in category j to produce, we require $\overline{\theta}_j c^{-1}(m_v \nu_j) \ge t$, and therefore $m_v \nu_j^* \equiv c(t/\overline{\theta}_j)$ is the critical mass for the category to remain active. The platform is viable only if $\nu_j \ge \nu_j^*$ for at least one category j. Similarly, in order for a category j to be popular enough to support any global influencers, we need $\frac{\overline{\theta}_j m_v \nu_j}{c'(c^{-1}(m_v))} \ge t$, and therefore $m_v \nu_j^{\ddagger} \equiv \frac{tc'(c^{-1}(m_v))}{\overline{\theta}_j}$ is the critical mass for this category to hatch a global influencer.

Corollary 2 (Critical Mass)

A category *j* is active on the platform only if $\nu_j \ge \nu_j^*$. A category *j* hatches fledgling (resp. global) influencers only if $\nu_j \ge \nu_j^{\dagger}$ (resp. $\nu_j \ge \nu_j^{\ddagger}$).



Figure 2: Four segments of creators on a $\nu_j - \theta$ panel, where $\overline{\theta}_j = \overline{\theta}$ for all j. $m_v \nu^*$ is the critical mass for a category to exist. $m_v \nu^{\dagger}$ (resp. $m_v \nu^{\ddagger}$) is the critical mass for a category to hatch fledgling (resp. global) influencers.

Figure 2 shows the four segments of creators across all possible θ and ν_j , where $\overline{\theta}_j = \overline{\theta}$ for all *j*. A category has to represent ν^* share of the viewer population in order to survive, and has to house ν^{\dagger} (resp. ν^{\dagger}) share to become a sufficiently popular category that hatches fledgling (resp. global) influencers.

3.3 Welfare Consequences

Having characterized the optimal algorithm that maximizes the ads income of the platform, we take a detour to contemplate on the welfare consequences of such modern algorithm that prevails the social media. Obviously, in the optimal algorithm, both sides of the users earn zero profit. The creators exert so much effort that they are on the verge of quitting. The viewers watch irrelevant contents and ads to the extent that they barely find the utility from reading worth their time.

Now suppose we consider a hypothetically benevolent platform, utilizing the algorithm to maximize users' welfare. To be specific, the users' welfare is a weight sum of creators' and viewers' net utility. As the weight varies, we obtain the Pareto frontier of what is achievable from an algorithm. Let $w_c, w_v > 0$ denote the Pareto weight on the creators and viewers, respectively.

We look for an obedient mechanism solving the following problem:

$$\max_{\substack{\{e_{j}^{\theta}\}_{\theta,j} \ge 0\\ \{\overline{a}_{j}^{\theta}, \underline{a}_{j}^{\theta}\}_{\theta,j} \in [0,1]^{2}}} w_{c} \sum_{j} \mu_{j} \int \left(m_{v} \left(\nu_{j} \overline{a}_{j}^{\theta} + (1 - \nu_{j}) \underline{a}_{j}^{\theta} \right) - c \left(e_{j}^{\theta} \right) \right) \mathrm{d}F(\theta|j)$$

$$+ w_{v} \sum_{j} \mu_{j} \int \left(\nu_{j} \overline{a}_{j}^{\theta} \theta e_{j}^{\theta} - t \left(\nu_{j} \overline{a}_{j}^{\theta} + (1 - \nu_{j}) \underline{a}_{j}^{\theta} \right) \right) \mathrm{d}F(\theta|j)$$

$$\text{st} \quad c \left(e^{\theta} \right) \leq m \left(\nu_{i} \overline{a}_{j}^{\theta} + (1 - \nu_{i}) a_{j}^{\theta} \right) \quad \forall \theta \ i$$

$$\tag{8}$$

 $c(e_j^{\circ}) \leqslant m_v \left(\nu_j a_j^{\circ} + (1 - \nu_j) \underline{a}_j^{\circ}\right), \ \forall \ \theta, j.$ (0)

Again, we consider the case where t is sufficiently small such that there exist $\{a_{i,k}^{\theta}\}_{\theta,j,k}$ consistent with \overline{a}_j and \underline{a}_j while (5) does not bind.

It appears that the welfare-maximizing algorithm crucially depends on the Pareto weights, in particular, the ratio of *payoff-adjusted* Pareto weights $\frac{tw_v}{w_c}$. We call it payoffadjusted because t is a viewer's cost of reading while 1 is a creator's normalized utility from attention. The ratio $\frac{tw_v}{w_c}$ thus weighs the social cost of reading against the social gain from the same action. The next result characterizes welfare-maximizing algorithms under different ratios.

Proposition 2 (Welfare Maximization) (*i*) When $\frac{tw_v}{w_c} \ge \frac{c'(c^{-1}(m_v\nu_j))c^{-1}(m_v\nu_j)}{m_v\nu_j}$ for all $j \in \mathcal{N}$, the welfare-maximizing algorithm assigns the same e_j^{θ} and $a_{j,k}^{\theta}$ as in the main model, but sets $A_k = 0$. (ii) When $1 < \frac{tw_v}{w_c} < \frac{c'(c^{-1}(m_v\nu_j))c^{-1}(m_v\nu_j)}{m_v\nu_j}$ for some $j \in \mathcal{N}$, the welfare-maximizing algorithm has a cutoff ability for local producers lower than that in the main model for category j, and some creators exert lower effort and enjoy positive utility.

(iii) When $\frac{tw_v}{w_c} \leq 1$, the welfare-maximizing algorithm has all θ producing, with $\overline{a}_j^{\theta} = \underline{a}_j^{\theta} = 1$.

Part (i) claims that when the benevolent platform sufficiently values the viewer side, the profit-maximizing algorithm can be readily used for welfare maximization too, except that there are no ads inserted in the recommendation. Intuitively, when the creators' utility has a low weight, they will be required to exert effort up to the limit of the participation constraint, which is also the case in the profit maximization. Given zero utility of the creators, the remaining problem is to maximize the viewers' utility, and that coincides with profit maximization too. Indeed, maximum ads is achieved by maximizing viewers' utility before cashing it out by inserting ads. By comparing the two algorithms, the source of inefficiency in the profit maximization is clear: viewers waste time on the ads. Other than that, there is no distortion on the production or the attention allocation on contents.

Part (ii) proposes a different algorithm when creators' utility becomes more important. As the platform now wants to leave some creators a positive net utility, it must be the lowest-ability active creators who should relax. After all, due to their low abilities, reducing the effort level has a smaller impact on the content quality than the same change on a high-ability creator. Moreover, since the entry-level creators only exert a reduced level of effort, it is efficient to set the cutoff ability lower. Therefore, the source of inefficiency in the profit maximization is now two fold. First, the requirement on ability to start producing is too high. Second, the low ability active creators exert too much effort. In short, the profit-maximizing algorithm is not inclusive enough, and is too demanding on the low ability creators.

4 Monetary Transfers

So far we do not allow for monetary transfers between the platform and the creators. The only source of utility for a creator is the attention he receives. In this extension we explicitly allow the platform to pay type-specific amount of money to the creators as an alternative method to incentivize them. In some platforms (e.g., YouTube and TikTok), this is the main reason for production.

In the obedient algorithm, when the platform recommends effort e_j^{θ} for a type- (θ, j) creator, it also promises a non-negative payment $\pi_j^{\theta} \ge 0$ if the recommendation is followed. We allow for any general payment schedule, including but not limiting to the linear pay-per-attention one. With similar arguments to Lemma 2, the obedience constraints are binding. The objective now reads:

$$\frac{zm_cm_v}{t}\sum_{j}\nu_j\mu_j\int\overline{a}_j^{\theta}\theta c^{-1}\left(\pi_j^{\theta}+m_v\nu_j\overline{a}_j^{\theta}+m_v(1-\nu_j)\underline{a}_j^{\theta}\right)\mathrm{d}F(\theta|j)$$
$$-zm_cm_v\sum_{j}\mu_j\int\left(\nu_j\overline{a}_j^{\theta}+(1-\nu_j)\underline{a}_j^{\theta}\right)\mathrm{d}F(\theta|j)-m_c\sum_{j}\mu_j\int\pi_j^{\theta}(1-\lambda_j^{\theta})\mathrm{d}F(\theta|j),\quad(9)$$

where λ_j^{θ} is the Lagrangian multiplier for $\pi_j^{\theta} \ge 0$. It turns out that positive payment is always used for high-ability creators, but depending on whether the market competitive price for ads is high or low, the optimal algorithm may or may not involve irrelevant attention.

4.1 High Ads Fee: z > 1

Since we normalize the utility from a unit of attention to 1, the condition $z \ge 1$ is a relative comparison that the ads fee per unit of attention is higher than the creator's utility per unit of attention. When this is the case, it is optimal to *never* recommend irrelevant contents. If the algorithm were to recommend some irrelevant contents from (θ, j) to k, then it can instead reduce a unit of them, free up space for one unit of ads in k's recommendation set, gather $z \ge 1$ dollars of ads fee, and pay creator (θ, j) one dollar to make up for the lost attention. Therefore, irrelevant attention is an inefficient channel to provide incentives. The next result characterizes the optimal algorithm with transfers.

Proposition 3 (Optimal Payment: High Ads Fee)

Suppose z > 1 and the attention cost t is sufficiently low. For each category $j \in \mathcal{N}$, there exists some $\hat{\theta}_j^*$ such that for $\theta < \hat{\theta}_j^*$, $e_j^{\theta} = 0$, $\overline{a}_j = 0$, $\underline{a}_j = 0$ and $\pi_j^{\theta} = 0$; for $\theta \ge \hat{\theta}_j^*$, $e_j^{\theta} = c^{-1}(m_v\nu_j)$, $\overline{a}_j = 1$, $\underline{a}_j = 0$ and $\pi_j^{\theta} = \max \{ c (c'^{-1} (\theta m_v z \nu_j / t)) - m_v \nu_j, 0 \}.$

According to the proposition, irrelevant attention $\underline{a}_j = 0$ for every creator. Moreover, the transfer is strictly increasing and convex in the creator's ability θ and the size of r relevant audience ν_j whenever it is positive, similar to that of irrelevant attention in the main model (Corollary 1). Indeed, it plays the role of a cheaper and unbounded version of of the latter. The lesson is that when the ads market pays a lucrative piece rate, the platform should feature accurate recommendation without irrelevant attention. It pays high ability creators (if not all), and the payment increases in the creator's ability and relevant audience size.

In practice, platforms share revenue with content creators by allocating a percentage of the advertising revenue generated from ads displayed on their content. One popular ad revenue-sharing model is to reward creators based on views. Proposition 3 suggests that for those creators who are paid, the optimal monetary transfer per attention unit,

$$\frac{\pi_j^{\theta}}{m_v \nu_j} = \frac{c \left(c'^{-1} \left(\theta m_v z \nu_j / t \right) \right)}{m_v \nu_j} - 1,$$

increases in the creator's ability and relevant audience size according to Corollary 1.

4.2 Low Ads Fee: z < 1

When the earnings from ads are low compared to the utility from attention, the platform should not rely solely on transfers. Instead, it will max out irrelevant attention before using money. The following result characterizes the optimal algorithm where other than the four existing segments of creators, there is a fifth segment: *paid* global influencers.

Proposition 4 (Optimal Payment: Low Ads Fee)

Suppose z < 1 and the attention cost t is sufficiently low. The optimal algorithm is the same as in Proposition 1 except that among global influencers, if additionally $\frac{\theta m_v \nu_j}{c'(c^{-1}(m_v))} > \frac{t}{z}$, then creator (θ, j) receives a positive payment $\pi_j^{\theta} = c \left(c'^{-1} \left(\theta m_v z \nu_j / t \right) \right) - m_v$.

Note that the condition for positive payment is stricter than that for global influencers due to z < 1. Therefore, there is a segment of unpaid global influencers because although they

deserve full attention from irrelevant viewers, their content quality is not high enough to justify payment which has a discretely higher cost. The proposition implies that when the ads market does not pay well, the algorithm should still deliberately use irrelevant attention as in the main model, and payment only occurs on very high-end global influencers. This aligns with the spirit of some ad revenue sharing programs like TikTok Pulse, which splits ad revenue only with creators whose videos rank in the top 4% of all TikTok content. Similar to the previous case, the optimal monetary transfer per attention unit for these global influencers $\pi_j^{\theta}/m_v = c \left(c'^{-1} \left(\theta m_v z \nu_j / t \right) \right) / m_v - 1$ increases in their ability and relevant audience size.

5 Conclusion

Social media has become an increasingly important part of many people's lives. The platforms of social media also fundamentally shape how information is created and distributed. In this paper we study a model with some crucial aspects of social media such as costly attention, directed attention by algorithm, vanity utility from attention, etc. We argue that since costly attention is a scarce resource to manage, the platform uses algorithms to meticulously allocate attention of the viewers and effort of the creators. When profit maximization is the goal of the designer, the optimal algorithm filters out low-ability creators, restricts medium-ability creators to niche audiences, and amplifies viral content from high-ability creators, creating a skewed distribution of attention. This naturally gives rise to a set of global influencers who is seen by all viewers, even if their specialization (horizontal location) does not necessarily fit all viewers. In contrast, when welfare maximization is the objective, the allocation of attention shifts away from prioritizing viral content and engagement-driven ad revenue. Instead, the platform broadens content exposure to better match viewers with creators who align with their preferences. This leads to a more inclusive ecosystem where low-ability creators are encouraged to participate. While global influencers still emerge, their dominance is reduced as the platform promotes a more diverse content landscape. Additionally, we explore how monetary transfers within the algorithm can mitigate some inefficiencies. Our results offer insights into the economics of content production, distribution, and consumption in digital markets, with direct implications for platform design, creator incentives, and regulatory interventions aimed at improving content allocation and market efficiency. Future research could explore how competition between platforms, alternative monetization models, or policy constraints influence these outcomes in digital markets.

Appendix: Proofs

Proof of Lemma 1. Given an arbitrary algorithm (\tilde{a}, \tilde{A}) , suppose an equilibrium features effort e_i^{θ} and reading share $\tilde{\alpha}_k$ of the recommendation set. Equilibrium requires:

$$\begin{split} e_{j}^{\theta} &\in \max_{e \geqslant 0} m_{v} \sum_{k} \nu_{k} \tilde{a}_{j,k}^{\theta}(\theta e) \tilde{\alpha}_{k} - c(e), \forall \ \theta, j, \\ m_{v} \sum_{k} \nu_{k} \tilde{a}_{j,k}^{\theta}(\theta e_{j}^{\theta}) \tilde{\alpha}_{k} - c(e_{j}^{\theta}) \geqslant 0, \forall \ \theta, j, \\ \tilde{\alpha}_{k} &\in \max_{\alpha \in [0,1]} \alpha m_{c} \mu_{k} \int \theta \tilde{a}_{k,k}^{\theta}(\theta e_{k}^{\theta}) e_{k}^{\theta} \mathrm{d}F(\theta|k) - \alpha t \cdot \left[m_{c} \sum_{j} \mu_{j} \int \tilde{a}_{j,k}^{\theta}(\theta e_{j}^{\theta}) \mathrm{d}F(\theta|j) + \tilde{A}_{k} \right], \forall \ k \\ \tilde{\alpha}_{k} m_{c} \mu_{k} \int \theta \tilde{a}_{k,k}^{\theta}(\theta e_{k}^{\theta}) e_{k}^{\theta} \mathrm{d}F(\theta|k) - \tilde{\alpha}_{k} t \cdot \left[m_{c} \sum_{j} \mu_{j} \int \tilde{a}_{j,k}^{\theta}(\theta e_{j}^{\theta}) \mathrm{d}F(\theta|j) + \tilde{A}_{k} \right] \geqslant 0, \forall \ k. \end{split}$$

Now consider a new mechanism, in which the platform recommends effort e_j^{θ} , promises attention assignment:

$$a_{j,k}^{\theta}(q) = \begin{cases} \tilde{a}_{j,k}^{\theta}(\theta e_j^{\theta})\tilde{\alpha}_k & \text{if} \quad q = \theta e_j^{\theta}, \\ 0 & \text{if} \quad q \neq \theta e_j^{\theta}. \end{cases},$$

ads assignment $A_k = \tilde{A}_k \alpha_k$, and recommends reading share $\alpha_k = 1$. Under the new mechanism, all constraints are satisfied:

$$\begin{split} e_{j}^{\theta} &\in \max_{e \geqslant 0} m_{v} \sum_{k} \nu_{k} a_{j,k}^{\theta}(\theta e) - c(e), \forall \ \theta, j, \\ m_{v} \sum_{k} \nu_{k} a_{j,k}^{\theta}(\theta e_{j}^{\theta}) - c(e_{j}^{\theta}) \geqslant 0, \forall \ \theta, j, \\ 1 &\in \max_{\alpha \in [0,1]} \alpha m_{c} \mu_{k} \int \theta a_{k,k}^{\theta}(\theta e_{k}^{\theta}) e_{k}^{\theta} \mathrm{d}F(\theta | k) - \alpha t \cdot \left[m_{c} \sum_{j} \mu_{j} \int a_{j,k}^{\theta}(\theta e_{j}^{\theta}) \mathrm{d}F(\theta | j) + A_{k} \right], \forall \ k, \\ m_{c} \mu_{k} \int \theta a_{k,k}^{\theta}(\theta e_{k}^{\theta}) e_{k}^{\theta} \mathrm{d}F(\theta | k) - t \cdot \left[m_{c} \sum_{j} \mu_{j} \int a_{j,k}^{\theta}(\theta e_{j}^{\theta}) \mathrm{d}F(\theta | j) + A_{k} \right] \geqslant 0, \forall \ k. \end{split}$$

Finally, rewrite $a_{j,k}^{\theta} \equiv a_{j,k}^{\theta}(\theta e_j^{\theta})$ to save notations.

Proof of Lemma 2. Suppose (2) is strict for some k. Then the platform should increase A_k to improve its profit. Now suppose (1) is strict for some (θ, j) . Then the platform can increase e_j^{θ} , which weakly relaxes (2) and weakly improves its profit. Therefore, (2) being binding is necessary for optimization, while (1) being binding is without loss of generality.

Proof of Lemma 3. Plug (4) into (3), and then take the derivative w.r.t. $a_{j,k}^{\theta}$. If $\theta e_j^{\theta} = 0$, then the derivative reads $-t\nu_k\mu_j f(\theta|j) < 0$, and we must have $a_{j,k}^{\theta} = 0$ for all k.

If $\theta e_j^{\theta} > 0$, then the derivative reads $\nu_k \mu_j f(\theta|j) \left(-t + \theta e_j^{\theta} + \frac{\theta}{c'(e_j^{\theta})} m_v \nu_j a_{j,j}^{\theta} \right)$ if k = j, and $\nu_k \mu_j f(\theta|j) \left(-t + \frac{\theta}{c'(e_j^{\theta})} m_v \nu_j a_{j,j}^{\theta} \right)$ if $k \neq j$.

(i) Suppose $\overline{a}_{j}^{\theta} = a_{j,j}^{\theta} = 0$. If $\theta e_{j}^{\theta} = 0$, then $a_{j,k}^{\theta} = 0$ for all $k \neq j$. If $\theta e_{j}^{\theta} > 0$, then $-t + \frac{\theta}{c'(e_{j}^{\theta})}m_{v}\nu_{j}a_{j,j}^{\theta} < -t + \theta e_{j}^{\theta} + \frac{\theta}{c'(e_{j}^{\theta})}m_{v}\nu_{j}a_{j,j}^{\theta} \leq 0$, and again $a_{j,k}^{\theta} = 0$ for all $k \neq j$. As a result, $\underline{a}_{j}^{\theta} = \frac{1}{1-\nu_{j}}\sum_{k\neq j}\nu_{k}a_{j,k}^{\theta} = 0$.

(ii) Suppose $\underline{a}_{j}^{\theta} > 0$, then there exists some $k \neq j$ s.t. $a_{j,k}^{\theta} > 0$, and $\theta e_{j}^{\theta} > 0$. Then $0 \leq -t + \frac{\theta}{c'(e_{j}^{\theta})} m_{v} \nu_{j} a_{j,j}^{\theta} < -t + \theta e_{j}^{\theta} + \frac{\theta}{c'(e_{j}^{\theta})} m_{v} \nu_{j} a_{j,j}^{\theta}$. As a result, $\overline{a}_{j}^{\theta} = a_{j,j}^{\theta} = 1$.

Proof of Proposition 1. Differentiating (6) w.r.t. $\overline{a}_{j}^{\theta}$ and $\underline{a}_{j}^{\theta}$, we have respectively:

$$f(\theta|j)\mu_{j}\nu_{j}\left(-t+\theta c^{-1}(m_{v}\nu_{j}\overline{a}_{j}^{\theta}+m_{v}(1-\nu_{j})\underline{a}_{j}^{\theta})+\frac{\theta m_{v}\nu_{j}\overline{a}_{j}^{\theta}}{c'(c^{-1}(m_{v}\nu_{j}\overline{a}_{j}^{\theta}+m_{v}(1-\nu_{j})\underline{a}_{j}^{\theta}))}\right)$$

$$f(\theta|j)\mu_{j}(1-\nu_{j})\left(-t+\frac{\theta m_{v}\nu_{j}\overline{a}_{j}^{\theta}}{c'(c^{-1}(m_{v}\nu_{j}\overline{a}_{j}^{\theta}+m_{v}(1-\nu_{j})\underline{a}_{j}^{\theta}))}\right).$$
(11)

Notice that (11) is strictly decreasing in $\underline{a}_{j}^{\theta}$ because c' and c^{-1} are both increasing. However, (10) is strictly increasing in $\overline{a}_{j}^{\theta}$ because the second derivative reads:

$$\frac{\theta m_v \nu_j}{c'(e_j^{\theta})^3} \left(2c'(e_j^{\theta})^2 - c(e_j^{\theta})c''(e_j^{\theta}) + m_v \underline{a}_j^{\theta} (1 - \nu_j)c''(e_j^{\theta}) \right) > 0,$$

where the inequality follows from the log-concavity of *c*. Therefore, the optimizer must feature $\overline{a}_j^{\theta} \in \{0, 1\}$. According to Lemma 3, $\underline{a}_j^{\theta} > 0$ implies $\overline{a}_j^{\theta} = 1$, and $\overline{a}_j^{\theta} = 0$ implies $\underline{a}_j^{\theta} = 0$.

Then we have potentially four cases. Case 3: $\overline{a}_j^{\theta} = 1$ and $\underline{a}_j^{\theta} \in (0, 1)$. (11) implies that $\underline{a}_j^{\theta} = \frac{c(c'^{-1}(\theta m_v \nu_j/t)) - m_v \nu_j}{m_v(1-\nu_j)}$ and we need $\theta \in (\theta_j^{\dagger}, \theta_j^{\ddagger})$ so that $\underline{a}_j^{\theta} \in (0, 1)$. Moreover, (6) must be higher than when $\overline{a}_j^{\theta} = \underline{a}_j^{\theta} = 0$, which boils down to $\frac{\theta m_v \nu_j}{t} c'^{-1} \left(\frac{\theta m_v \nu_j}{t}\right) \ge c \left(c'^{-1} \left(\frac{\theta m_v \nu_j}{t}\right)\right)$. This is always true because $xc'^{-1}(x) - c(c'^{-1}(x)) \equiv \int_0^x c'^{-1}(x') dx' > 0$ for all x > 0. Note that $\theta_j^{\dagger} < \theta_j^{\ddagger}$ because $\nu_j < 1$ and c' and c^{-1} are strictly increasing.

Case 4: $\overline{a}_j^{\theta} = 1$ and $\underline{a}_j^{\theta} = 1$. (11) implies $\theta \ge \theta_j^{\ddagger}$. Moreover, (6) must be higher than when $\overline{a}_j^{\theta} = \underline{a}_j^{\theta} = 0$, which boils down to $\theta \nu_j c^{-1}(m_v) \ge t$. This is always true for $\theta \ge \theta_j^{\ddagger}$ because we can set $x = c'(c^{-1}(m_v))$ and use the inequality $xc'^{-1}(x) - c(c'^{-1}(x)) > 0$ for all x > 0.

Case 2: $\overline{a}_{j}^{\theta} = 1$ and $\underline{a}_{j}^{\theta} = 0$. (11) implies $\theta \leq \theta_{j}^{\dagger}$. Moreover, (6) must be higher than when $\overline{a}_{j}^{\theta} = \underline{a}_{j}^{\theta} = 0$, which boils down to $\theta > \theta_{j}^{*}$. Note that $\theta_{j}^{*} < \theta_{j}^{\dagger}$ because we can set $x = c'(c^{-1}(m_{v}\nu_{j}))$ and use the inequality $xc'^{-1}(x) - c(c'^{-1}(x)) > 0$ for all x > 0.

Case 1: $\bar{a}_j^{\theta} = \underline{a}_j^{\theta} = 0$. We only require (6) to be higher than when $\bar{a}_j^{\theta} = 1$ and \underline{a}_j^{θ} is optimally chosen. If $\underline{a}_j^{\theta} > 0$, this is impossible from the analysis of Cases 3 and 4.

Therefore, $\underline{a}_{j}^{\theta} = 0$, and the comparison boils down to $\theta \leq \theta_{j}^{*}$. Since t > 0, we have $\theta_{j}^{*} > 0$.

Proof of Corollary 1. The total attention for a fledgling influencer (θ, j) is $m_v(\overline{a}_j^{\theta}\nu_j + \underline{a}_j^{\theta}(1-\nu_j)) = c\left(c'^{-1}(\theta m_v\nu_j/t)\right)$.

Note that:

$$\frac{\mathrm{d}}{\mathrm{d}\theta} \frac{c\left(c'^{-1}(\theta m_v \nu_j/t)\right)}{\theta} = \frac{c'(x)^2 - c(x)c''(x)}{\theta^2 c''(x)} > 0.$$

where $x = c'^{-1}(\theta m_v \nu_j / t)$. The inequality comes from the log-concavity of c. Considering the symmetry between θ and ν_j in $c(c'^{-1}(\theta m_v \nu_j / t))$, the proof for $\frac{c(c'^{-1}(\theta m_v \nu_j / t))}{\nu_j}$ is similar.

Proof of Corollary 2. If a category *j* supports active creators, we must have $\theta_j^* \leq \overline{\theta}_j$. By definition, this means $\overline{\theta}_j c^{-1}(m_v \nu_j) \geq t$, or equivalently $m_v \nu_j \geq c(t/\overline{\theta}_j)$. Therefore, $\nu_j \geq \nu_j^*$.

Similarly, if a category j hatches global influencers, we must have $\theta_j^{\ddagger} \leq \overline{\theta}_j$. By definition, this means $\frac{\overline{\theta}_j m_v \nu_j}{c'(c^{-1}(m_v))} \geq t$, or equivalently $m_v \nu_j \geq \frac{tc'(c^{-1}(m_v))}{\overline{\theta}_j}$. Therefore, $\nu_j \geq \nu_j^{\ddagger}$.

Proof of Proposition 2. In welfare maximization, Lemma 3 still holds. Denote the Lagrangian multiplier for (8) as $w_c \lambda_i^{\theta} \ge 0$. The first order condition w.r.t. e_i^{θ} requires:

$$e_j^{\theta} = c'^{-1} \left(\frac{\theta m_v w_v \nu_j \overline{a}_j^{\theta}}{w_c (1 + \lambda_j^{\theta})} \right)$$

(i) We first examine conditions under which (8) always holds with equality. Note that when this is the case, the objective reduces to the one in the main model and the candidate solution is the same as in the main model. In particular, $e_j^{\theta} = c^{-1}(m_v(\overline{a}_j^{\theta}\nu_j + \underline{a}_j^{\theta}(1 - \nu_j)))$. When $\theta < \theta_j^*$, we have $\overline{a}_j^{\theta} = \underline{a}_j^{\theta} = 0$, and the two expressions for e_j^{θ} trivially coincide. When $\theta \ge \theta_j^*$, we know $\overline{a}_j^{\theta} = 1$. Then, $\lambda_j^{\theta} \ge 0$ means:

$$c'^{-1}\left(\frac{\theta m_v w_v \nu_j \overline{a}_j^{\theta}}{w_p}\right) \leqslant c^{-1}(m_v(\overline{a}_j^{\theta} \nu_j + \underline{a}_j^{\theta}(1-\nu_j)))$$

for all $\theta \ge \theta_j^*$. Given the solution to the main model, the necessary and sufficient condition is $\frac{tw_v}{w_c} \ge \frac{c'(c^{-1}(m_v\nu_j))c^{-1}(m_v\nu_j)}{m_v\nu_j}$.

(ii) Suppose $1 < \frac{tw_v}{w_c} < \frac{c'(c^{-1}(m_v\nu_j))c^{-1}(m_v\nu_j)}{m_v\nu_j}$ for some j. Plugging in the effort e_j^{θ} from the first order condition, the derivative of (7) w.r.t. \underline{a}_j^{θ} yields $m_vw_c(1-\nu_j)(1-\frac{tw_v}{w_c}+\lambda_j^{\theta})$. If $\theta > \theta_j^{\dagger}$ and $\lambda_j^{\theta} = 0$, then $\underline{a}_j^{\theta} = 0$, $\overline{a}_j^{\theta} = 1$ and the candidate e_j^{θ} violates (8). Therefore, $\lambda_j^{\theta} > 0$ and we end up with Cases 3 and 4 in Proposition 1. If $\frac{w_c}{w_v} \frac{c'(c^{-1}(m_v\nu_j))}{m_v\nu_j} < \theta < \theta_j^{\dagger}$ and $\lambda_j^{\theta} = 0$, then the same contradiction arises. Therefore, $\lambda_j^{\theta} > 0$ and we end up with Cases 2 in Proposition 1. If $\theta \leqslant \frac{w_c}{w_v} \frac{c'(c^{-1}(m_v\nu_j))}{m_v\nu_j}$, then regardless of λ_j^{θ} we must have $\underline{a}_j^{\theta} = 0$. If $\overline{a}_j^{\theta} = 1$

then (8) is not binding. This, compared to $\overline{a}_j^{\theta} = 0$, produces a higher objective if and only if $\theta \ge \tilde{\theta}_j^*$, where $\tilde{\theta}_j^* > 0$ uniquely solves

$$\int_{0}^{\hat{\theta}_{j}^{*}w_{v}m_{v}\nu_{j}/w_{c}} c'^{-1}(x) \mathrm{d}x = m_{v}\nu_{j}\left(\frac{tw_{v}}{w_{c}} - 1\right).$$

Finally, we want to show $\tilde{\theta}_j^* < \theta_j^*$. We know $\tilde{\theta}_j^* > 0$ satisfies:

$$m_v \nu_j \left(\frac{tw_v}{w_c} - 1\right) + c \left(c'^{-1} \left(\frac{\tilde{\theta}_j^* m_v w_v \nu_j}{w_c}\right)\right) - \frac{\tilde{\theta}_j^* m_v w_v \nu_j}{w_c} c'^{-1} \left(\frac{\tilde{\theta}_j^* m_v w_v \nu_j}{w_c}\right) = 0.$$

Replacing $\tilde{\theta}_i^*$ with θ_i^* and taking the derivative of the left-hand side w.r.t. *t*, we have:

$$\frac{m_v w_v \nu_j}{c^{-1}(m_v \nu_j)} \left(c^{-1}(m_v \nu_j) - c'^{-1} \left(\frac{t w_v m_v \nu_j}{w_c c^{-1}(m_v \nu_j)} \right) \right) > 0$$

for $\frac{tw_v}{w_c} < \frac{c'(c^{-1}(m_v\nu_j))c^{-1}(m_v\nu_j)}{m_v\nu_j}$, and the left-hand side becomes zero when $\frac{tw_v}{w_c} = \frac{c'(c^{-1}(m_v\nu_j))c^{-1}(m_v\nu_j)}{m_v\nu_j}$. Therefore, the left-hand side is negative for $\frac{tw_v}{w_c} < \frac{c'(c^{-1}(m_v\nu_j))c^{-1}(m_v\nu_j)}{m_v\nu_j}$. Since $xc'^{-1}(x) - c(c'^{-1}(x))$ increases in x > 0, we know that $\theta_j^* > \tilde{\theta}_j^*$.

(iii) Suppose $\frac{tw_v}{w_c} \leq 1$ for some j. Then according to the derivatives of (7) w.r.t. \overline{a}_j^{θ} and \underline{a}_j^{θ} yields $\overline{a}_j^{\theta} = \underline{a}_j^{\theta} = 1$ for all θ . In order for (8) to bind, we need $\theta > \frac{w_c}{w_v} \frac{c'(c^{-1}(m_v))}{m_v \nu_j}$.

Proof of Proposition 3. Plugging the first order condition w.r.t. π_j^{θ} into the derivatives w.r.t. \overline{a}_j^{θ} and \underline{a}_j^{θ} , we have $tm_v\nu_j(1-z+\frac{\theta e_j^{\theta}z}{t}-\lambda_j^{\theta})$ increasing in \overline{a}_j^{θ} , and $tm_v(1-\nu_j)(1-z-\lambda_j^{\theta}) < 0$. This means $\underline{a}_j^{\theta} = 0$ for all θ , and $\overline{a}_j^{\theta} \in \{0, 1\}$.

If $\overline{a}_j^{\theta} = 0$, then the first order condition w.r.t. π_j^{θ} requires $\pi_j^{\theta} = 0$. If $\overline{a}_j^{\theta} = 1$, then $\pi_j^{\theta} = c \left(c'^{-1} \left(\frac{\theta z m_v \nu_j}{t(1-\lambda_j^{\theta})} \right) \right) - m_v \nu_j$. Comparing the two cases, the objective is greater if and only if

$$\frac{z}{t}m_v\nu_j\left(\theta c^{-1}(\pi_j^\theta + m_v\nu_j) - t\right) > \pi_j^\theta.$$
(12)

When $z \ge \frac{c'(c'^{-1}(m_v\nu_j))c'^{-1}(m_v\nu_j)}{m_v\nu_j}$, (12) must imply $\lambda_j^{\theta} = 0$. If not, then $\pi_j^{\theta} = 0$ and (12) reduces to $\theta > \theta_j^*$. Given this, $\pi_j^{\theta} > 0$, a contradiction. Therefore, $\overline{a}_j^{\theta} = 1$ whenever $\theta > \hat{\theta}_j^*$, where $\hat{\theta}_j^*$ uniquely solves

$$\int_0^{\hat{\theta}_j^* z m_v \nu_j / t} c'^{-1}(x) \mathrm{d}x = m_v \nu_j (z - 1).$$

Now suppose $z < \frac{c'(c'^{-1}(m_v\nu_j))c'^{-1}(m_v\nu_j)}{m_v\nu_j}$. For $\theta \ge \frac{tc'(c^{-1}(m_v\nu_j))}{zm_v\nu_j}$, (12) must imply $\lambda_j^{\theta} = 0$ for the same reason as above. For $\theta_j^* \le \theta < \frac{tc'(c^{-1}(m_v\nu_j))}{zm_v\nu_j}$, (12) must imply $\lambda_j^{\theta} > 0$. If not, then

 $\lambda_j^{\theta} = 0$ and $\pi_j^{\theta} < 0$, a contradiction. For $\theta < \theta_j^*$, (12) is violated. Therefore, $\hat{\theta}_j^* = \theta_j^*$.

Proof of Proposition 4. Plugging the first order condition w.r.t. π_j^{θ} into the derivatives w.r.t. \overline{a}_j^{θ} and \underline{a}_j^{θ} , we have $tm_v\nu_j(1-z+\frac{\theta e_j^{\theta}z}{t}-\lambda_j^{\theta})$ increasing in \overline{a}_j^{θ} , and $tm_v(1-\nu_j)(1-z-\lambda_j^{\theta})$. This means $\overline{a}_j^{\theta} \in \{0,1\}$.

For $\theta \leq \frac{\theta_j^{\dagger}}{z}$, if $\pi_j^{\theta} > 0$, then $\lambda_j^{\theta} = 0$. This implies $\underline{a}_j^{\theta} = \overline{a}_j^{\theta} = 1$. However, the first order condition w.r.t. π_j^{θ} requires

$$\pi_j^{\theta} = c \left(c'^{-1} \left(\frac{\theta z m_v \nu_j \overline{a}_j^{\theta}}{t(1 - \lambda_j^{\theta})} \right) \right) - m_v (\overline{a}_j^{\theta} \nu_j + \underline{a}_j^{\theta} (1 - \nu_j)) = c \left(c'^{-1} \left(\frac{z \theta}{\theta_j^{\ddagger}} c'(c^{-1}(m_v)) \right) \right) - m_v \leqslant 0,$$

a contradiction. Therefore, $\pi_j^{\theta} = 0$ for all $\theta \leq \frac{\theta_j^{\dagger}}{z}$, and the solution is the same as the main model for these θ .

For $\theta > \frac{\theta_j^{\dagger}}{z}$, we must have $\pi_j^{\theta} > 0$. If not, then $\overline{a}_j^{\theta} = \underline{a}_j^{\theta} = 1$ according to Proposition 1. However,

$$\pi_j^{\theta} = 0 > c \left(c'^{-1} \left(\frac{\theta_j^{\dagger} m_v \nu_j}{t} \right) \right) - m_v = 0,$$

a contradiction. Therefore, $\pi_j^{\theta} > 0$ for all $\theta > \frac{\theta_j^{\dagger}}{z}$, and since $\lambda_j^{\theta} = 0$, we know $\overline{a}_j^{\theta} = \underline{a}_j^{\theta} = 1$.

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